

# Package ‘AsyK’

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**Type** Package

**Title** Kernel Density Estimation

**Version** 1.5.6

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**Description** A collection of functions related to density estimation by using Chen's (2000) idea. Mean Squared Errors (MSE) are calculated for estimated curves. For this purpose, R functions allow the distribution to be Gamma, Exponential or Weibull. For details see Chen (2000), Scaillet (2004) <doi:10.1080/10485250310001624819> and Khan and Akbar.

**License** GPL-2

**Encoding** UTF-8

**RoxygenNote** 7.3.2

**URL** <https://CRAN.R-project.org/package=AsyK>

**NeedsCompilation** no

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 AsyK-package

 AsyK
 

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### Description

A collection of functions related to density estimation by using Chen's (2000) idea. For observing estimated values see [Laplace](#) and [RIG](#). Plots by using these kernels can be drawn by [plot.Laplace](#) and [plot.RIG](#). Mean squared errors (MSE) can be calculated by [mse](#). Here we also present a normal scale rule bandwidth which is given by Silverman (1986) for non-normal data.

### Details

Kernel Density Estimation

### Author(s)

Javaria Ahmad Khan, Atif Akbar.

### See Also

Useful links:

- <https://CRAN.R-project.org/package=AsyK>

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 Laplace

*Estimate Density Values by Laplace kernel*


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### Description

Estimated Kernel density values by using Laplace Kernel.

### Usage

```
Laplace(x = NULL, y, k = NULL, h = NULL)
```

### Arguments

x	scheme for generating grid points
y	a numeric vector of positive values.
k	grid points.
h	the bandwidth

**Details**

Laplace kernel is developed by Khan and Akbar. Kernel is developed by using Chen's idea. Laplace kernel is;

$$K_{Laplace(x, h^{\frac{1}{2}})}(u) = \frac{1}{2\sqrt{h}} \exp\left(-\frac{|u-x|}{\sqrt{h}}\right)$$

**Value**

x	grid points
y	estimated values of density

**Author(s)**

Javaria Ahmad Khan, Atif Akbar.

**References**

Khan, J. A.; Akbar, A. Density Estimation by Laplace Kernel. *Working paper, Department of Statistics, Bahauddin Zakariya University, Multan, Pakistan.*

**See Also**

To examine Laplace density plot see [plot.Laplace](#) and for Mean Squared Error [mse](#). Similarly, for RIG kernel [RIG](#).

**Examples**

```
#Data can be simulated or real data
## Number of grid points "k" should be at least equal to the data size.
### If user define the generating scheme of gridpoints than number of gridpoints should
####be equal or greater than "k"
##### otherwise NA will be produced.
y <- rexp(100, 1)
xx <- seq(min(y) + 0.05, max(y), length = 100)
h <- 2
den <- Laplace(x = xx, y = y, k = 200, h = h)

##If scheme for generating gridpoints is unknown
y <- rexp(50, 1)
h <- 3
den <- Laplace(y = y, k = 90, h = h)

##If user do not mention the number of grid points
y <- rexp(23, 1)
xx <- seq(min(y) + 0.05, max(y), length = 90)

## Not run:
#any bandwidth can be used
require(KernSmooth)
h <- dpik(y)
den <- Laplace(x = xx, y = y, h = h)
```

```
## End(Not run)

#if bandwidth is missing
y <- rexp(100, 1)
xx <- seq(min(y) + 0.05, max(y), length = 100)
den <- Laplace(x = xx, y = y, k = 90)
```

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mse

*Calculate Mean Squared Error( MSE) by using different Kernels*

---

### Description

This function calculates the mean squared error (MSE) by using user specified kernel. This function is same as provided in package "DELTD". For details see <https://CRAN.R-project.org/package=DELTD>.

### Usage

```
mse(kernel, type)
```

### Arguments

kernel	type of kernel which is to be used
type	mention distribution of vector. If exponential distribution then use "Exp". If use gamma distribution then use "Gamma". If Weibull distribution then use "Weibull".

### Value

Mean Squared Error (MSE)

### Author(s)

Javaria Ahmad Khan, Atif Akbar.

### References

<https://CRAN.R-project.org/package=DELTD>

### See Also

This is also available in **DELTD**

**Examples**

```
y <- rexp(100, 1)
xx <- seq(min(y) + 0.05, max(y), length = 500)
h <- 2
gr <- Laplace(x = xx, y = y, k = 200, h = h)
mse(kernel = gr, type = "Exp")
## if distribution is other than mentioned \code{type} is used then NaN will be produced.
## Not run:
mse(kernel = gr, type = "Beta")

## End(Not run)
```

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NSR

*Calculate Bandwidth proposed by Silverman for non-normal data.*

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**Description**

Calculate Bandwidth proposed by Silverman for non-normal data.

**Usage**

```
NSR(y)
```

**Arguments**

y                    a numeric vector of positive values.

**Value**

h

**Author(s)**

Javaria Ahmad Khan, Atif Akbar.

**References**

Silverman, B. W. 1986. *Density Estimation*. Chapman & Hall/ CRC, London.

**Examples**

```
y <- rexp(10, 1)
NSR(y)
```

---

plot.Laplace

*Density Plot by Laplace kernel*


---

**Description**

Plot density by using Laplace Kernel.

**Usage**

```
## S3 method for class 'Laplace'
plot(x, ...)
```

**Arguments**

x                    an object of class "Laplace"  
...                    Not presently used in this implementation

**Value**

nothing

**Author(s)**

Javaria Ahmad Khan, Atif Akbar.

**References**

Khan, J. A.; Akbar, A. Density Estimation by Laplace Kernel. *Working paper, Department of Statistics, Bahauddin Zakariya University, Multan, Pakistan.*

**See Also**

To examine Laplace estimated values for density see [Laplace](#) and for Mean Squared Error [mse](#). Similarly, for plot of Laplace kernel [plot.RIG](#).

**Examples**

```
y <- rexp(100, 1)
h <- 0.79 * IQR(y) * length(y) ^ (-1/5)
xx <- seq(min(y) + 0.05, max(y), length = 100)
den <- Laplace(x = xx, y = y, k = 100, h = h)
plot(den, type = "l")

##other details can also be added
y <- rexp(100, 1)
h <- 0.79 * IQR(y) * length(y) ^ (-1/5)
den <- Laplace(x = xx, y = y, k = 100, h = h)
plot(den, type = "s", ylab = "Density Function", lty = 1, xlab = "Time")
```

```
## To add true density along with estimated
d1 <- density(y, bw = h)
lines(d1, type = "p", col = "red")
legend("topright", c("Real Density", "Density by RIG Kernel"),
col = c("red", "black"), lty = c(1, 2))
```

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plot.RIG

*Density Plot by Reciprocal Inverse Gaussian kernel*

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### Description

Plot density by using Reciprocal Inverse Gaussian Kernel.

### Usage

```
## S3 method for class 'RIG'
plot(x, ...)
```

### Arguments

x                    an object of class "RIG"  
...                   Not presently used in this implementation

### Value

nothing

### Author(s)

Javaria Ahmad Khan, Atif Akbar.

### References

Scaillet, O. 2004. Density estimation using inverse and reciprocal inverse Gaussian kernels. *Non-parametric Statistics*, **16**, 217-226.

### See Also

To examine RIG estimated values for density see [RIG](#) and for Mean Squared Error [mse](#). Similarly, for plot of Laplace kernel [plot.Laplace](#).

**Examples**

```

y <- rexp(200, 1)
h <- 0.79 * IQR(y) * length(y) ^ (-1/5)
xx <- seq(min(y) + 0.05, max(y), length = 200)
den <- RIG(x = xx, y = y, k = 200, h = h)
plot(den, type = "l")

##other details can also be added
y <- rexp(200, 1)
h <- 0.79 * IQR(y) * length(y) ^ (-1/5)
den <- RIG(x = xx, y = y, k = 200, h = h)
plot(den, type = "s", ylab = "Density Function", lty = 1, xlab = "Time")

## To add true density along with estimated
d1 <- density(y, bw = h)
lines(d1, type = "p", col = "red")
legend("topright", c("Real Density", "Density by RIG Kernel"),
col = c("red", "black"), lty = c(1, 2))

```

RIG

*Estimated Density Values by Reciprocal Inverse Gaussian kernel***Description**

Estimated Kernel density values by using Reciprocal Inverse Gaussian Kernel.

**Usage**

```
RIG(x = NULL, y, k = NULL, h = NULL)
```

**Arguments**

x	scheme for generating grid points
y	a numeric vector of positive values.
k	grid points.
h	the bandwidth

**Details**

Scaillet 2003. proposed Reciprocal Inverse Gaussian kernel. He claimed that his proposed kernel share the same properties as those of gamma kernel estimator.

$$K_{RIG(\ln ax^4 \ln(\frac{1}{h}))}(y) = \frac{1}{\sqrt{2\pi y}} \exp \left[ -\frac{x-h}{2h} \left( \frac{y}{x-h} - 2 + \frac{x-h}{y} \right) \right]$$



**Value**

x	grid points
y	estimated values of density

**Author(s)**

Javaria Ahmad Khan, Atif Akbar.

**References**

Scaillet, O. 2004. Density estimation using inverse and reciprocal inverse Gaussian kernels. *Non-parametric Statistics*, **16**, 217-226.

**See Also**

To examine RIG density plot see [plot.RIG](#) and for Mean Squared Error [mse](#). Similarly, for Laplace kernel [Laplace](#).

**Examples**

```
#Data can be simulated or real data
## Number of grid points "k" should be at least equal to the data size.
### If user define the generating scheme of gridpoints than number of gridpoints should
####be equal or greater than "k"
##### otherwise NA will be produced.
y <- rexp(100, 1)
xx <- seq(min(y) + 0.05, max(y), length = 100)
h <- 2
den <- RIG(x = xx, y = y, k = 200, h = h)

##If scheme for generating gridpoints is unknown
y <- rexp(50, 1)
h <- 3
den <- RIG(y = y, k = 90, h = h)

## Not run:
##If user do not mention the number of grid points
y <- rexp(23, 1)
xx <- seq(min(y) + 0.05, max(y), length = 90)
#any bandwidth can be used
require(KernSmooth)
h <- dpik(y)
den <- RIG(x = xx, y = y, h = h)

## End(Not run)
#if bandwidth is missing
y <- rexp(100, 1)
xx <- seq(min(y) + 0.05, max(y), length = 100)
den <- RIG(x = xx, y = y, k = 90)
```

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