

# Package ‘BsMD’

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**Title** Bayes Screening and Model Discrimination

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**Description** Bayes screening and model discrimination follow-up designs.

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BsMD-package

*Bayes screening and model discrimination follow-up designs*

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### Description

Bayes screening and model discrimination follow-up designs

### Details

Package: BsMD  
Type: Package  
Version: 2023.920  
Date: 2023-09-14  
License: GPL version 2 or later

The packages allows you to perform the calculations and analyses described in Mayer, Stainberg and Box paper in Technometrics, 1996.

### Author(s)

Author: Ernesto Barrios based on Daniel Meyer's code. Maintainer: Ernesto Barrios <ebarrios@itam.mx>

### References

Box and Mayer, 1986; Box and Mayer, 1993; Mayer, Steinberg and Box, 1996.

### Examples

```
data(BM86.data)
```

---

BM86.data

*Data sets in Box and Meyer (1986)*

---

### Description

Design factors and responses used in the examples of Box and Meyer (1986)

### Usage

```
data(BM86.data)
```

**Format**

A data frame with 16 observations on the following 19 variables.

- X1** numeric vector. Contrast factor.
- X2** numeric vector. Contrast factor.
- X3** numeric vector. Contrast factor.
- X4** numeric vector. Contrast factor.
- X5** numeric vector. Contrast factor.
- X6** numeric vector. Contrast factor.
- X7** numeric vector. Contrast factor.
- X8** numeric vector. Contrast factor.
- X9** numeric vector. Contrast factor.
- X10** numeric vector. Contrast factor.
- X11** numeric vector. Contrast factor.
- X12** numeric vector. Contrast factor.
- X13** numeric vector. Contrast factor.
- X14** numeric vector. Contrast factor.
- X15** numeric vector. Contrast factor.
- y1** numeric vector. Log drill advance response.
- y2** numeric vector. Tensile strength response.
- y3** numeric vector. Shrinkage response.
- y4** numeric vector. Yield of isatin response.

**Source**

Box, G. E. P and R. D. Meyer (1986). "An Analysis of Unreplicated Fractional Factorials". *Technometrics*. Vol. 28. No. 1. pp. 11–18.

**Examples**

```
library(BsMD)
data(BM86.data, package="BsMD")
print(BM86.data)
```

---

BM93.e1.data

*Example 1 data in Box and Meyer (1993)*

---

### Description

12-run Plackett-Burman design from the  $2^5$  reactor example from Box, Hunter and Hunter (1977).

### Usage

```
data(BM93.e1.data)
```

### Format

A data frame with 12 observations on the following 7 variables.

**Run** a numeric vector. Run number from a  $2^5$  factorial design in standard order.

**A** a numeric vector. Feed rate factor.

**B** a numeric vector. Catalyst factor.

**C** a numeric vector. Agitation factor.

**D** a numeric vector. Temperature factor.

**E** a numeric vector. Concentration factor.

**y** a numeric vector. Percent reacted response.

### Source

Box G. E. P, Hunter, W. C. and Hunter, J. S. (1978). *Statistics for Experimenters*. Wiley.

Box, G. E. P and R. D. Meyer (1993). "Finding the Active Factors in Fractionated Screening Experiments". *Journal of Quality Technology*. Vol. 25. No. 2. pp. 94–105.

### Examples

```
library(BsMD)
data(BM93.e1.data, package="BsMD")
print(BM93.e1.data)
```

---

BM93.e2.data

*Example 2 data in Box and Meyer (1993)*

---

### Description

12-run Plackett-Burman design for the study of fatigue life of weld repaired castings.

### Usage

```
data(BM93.e2.data)
```

### Format

A data frame with 12 observations on the following 8 variables.

**A** a numeric vector. Initial structure factor.

**B** a numeric vector. Bead size factor.

**C** a numeric vector. Pressure treat factor.

**D** a numeric vector. Heat treat factor.

**E** a numeric vector. Cooling rate factor.

**F** a numeric vector. Polish factor.

**G** a numeric vector. Final treat factor.

**y** a numeric vector. Natural log of fatigue life response.

### Source

Hunter, G. B., Hodi, F. S., and Eager, T. W. (1982). "High-Cycle Fatigue of Weld Repaired Cast Ti-6Al-4V". *Metallurgical Transactions* 13A, pp. 1589–1594.

Box, G. E. P and R. D. Meyer (1993). "Finding the Active Factors in Fractionated Screening Experiments". *Journal of Quality Technology*. Vol. 25. No. 2. pp. 94–105.

### Examples

```
library(BsMD)
data(BM93.e2.data,package="BsMD")
print(BM93.e2.data)
```

---

BM93.e3.data

*Example 3 data in Box and Meyer (1993)*

---

### Description

$2^{8-4}$  Fractional factorial design in the injection molding example from Box, Hunter and Hunter (1978).

### Usage

```
data(BM93.e3.data)
```

### Format

A data frame with 20 observations on the following 10 variables.

**blk** a numeric vector

**A** a numeric vector. Mold temperature factor.

**B** a numeric vector. Moisture content factor.

**C** a numeric vector. Holding Pressure factor.

**D** a numeric vector. Cavity thickness factor.

**E** a numeric vector. Booster pressure factor.

**F** a numeric vector. Cycle time factor.

**G** a numeric vector. Gate size factor.

**H** a numeric vector. Screw speed factor.

**y** a numeric vector. Shrinkage response.

### Source

Box G. E. P, Hunter, W. C. and Hunter, J. S. (1978). *Statistics for Experimenters*. Wiley.

Box G. E. P, Hunter, W. C. and Hunter, J. S. (2004). *Statistics for Experimenters II*. Wiley.

Box, G. E. P and R. D. Meyer (1993). "Finding the Active Factors in Fractionated Screening Experiments". *Journal of Quality Technology*. Vol. 25. No. 2. pp. 94–105.

### Examples

```
library(BsMD)
data(BM93.e3.data, package="BsMD")
print(BM93.e3.data)
```

**Description**

Marginal factor posterior probabilities and model posterior probabilities from designed screening experiments are calculated according to Box and Meyer's Bayesian procedure.

**Usage**

```
BsProb(X, y, blk, mFac, mInt = 2, p = 0.25, g = 2, ng = 1, nMod = 10)
```

**Arguments**

|      |  |
|------|--|
| X    | Matrix. The design matrix.   |
| y    | vector. The response vector.   |
| blk  | integer. Number of blocking factors ( $\geq 0$ ). These factors are accommodated in the first columns of matrix X. There are $\text{ncol}(X) - \text{blk}$ design factors. |
| mFac | integer. Maximum number of factors included in the models.   |
| mInt | integer $\leq 3$ . Maximum order of interactions considered in the models.   |
| p    | numeric. Prior probability assigned to active factors.   |
| g    | vector. Variance inflation factor(s) $\gamma$ associated to active and interaction factors.  |
| ng   | integer $\leq 20$ . Number of different variance inflation factors (g) used in calculations.   |
| nMod | integer $\leq 100$ . Number of models to keep with the highest posterior probability.  |

**Details**

Factor and model posterior probabilities are computed by Box and Meyer's Bayesian procedure. The design factors are accommodated in the matrix X after blk columns of the blocking factors. So,  $\text{ncol}(X) - \text{blk}$  design factors are considered. If g, the variance inflation factor (VIF)  $\gamma$ , is a vector of length 1, the same VIF is used for factor main effects and interactions. If the length of g is 2 and ng is 1, g[1] is used for factor main effects and g[2] for the interaction effects. If ng greater than 1, then ng values of VIFs between g[1] and g[2] are used for calculations with the same *gamma* value for main effects and interactions. The function calls the FORTRAN subroutine 'bm' and captures summary results. The complete output of the FORTRAN code is save in the 'BsPrint.out' file in the working directory. The output is a list of class BsProb for which print, plot and summary methods are available.

**Value**

A list with all output parameters of the FORTRAN subroutine 'bm'. The names of the list components are such that they match the original FORTRAN code. Small letters used for capturing program's output.

|        |  |
|--------|--|
| X      | matrix. The design matrix.   |
| Y      | vector. The response vector.   |
| N      | integer. The number of runs.   |
| COLS   | integer. The number of design factors.   |
| BLKS   | integer. The number of blocking factors accommodated in the first columns of matrix X.   |
| MXFAC  | integer. Maximum number of factors considered in the models.   |
| MXINT  | integer. Maximum interaction order considered in the models.   |
| PI     | numeric. Prior probability assigned to the active factors.   |
| INDGAM | integer. If 0, the same variance inflation factor (GAMMA) is used for main and interactions effects. If INDGAM ==1, then NGAM different values of GAMMA were used.     |
| INDG2  | integer. If 1, the variance inflation factor GAM2 was used for the interaction effects.  |
| NGAM   | integer. Number of different VIFs used for computations.   |
| GAMMA  | vector. Vector of variance inflation factors of length 1 or 2.   |
| NTOP   | integer. Number of models with the highest posterior probability   |
| .      |  |
| mdcnt  | integer. Total number of models evaluated.   |
| ptop   | vector. Vector of probabilities of the top ntop models.  |
| sigtop | vector. Vector of sigma-squared of the top ntop models.  |
| nftop  | integer. Number of factors in each of the ntop models.   |
| jtop   | matrix. Matrix of the number of factors and their labels of the top ntop models.   |
| del    | numeric. Interval width of the GAMMA partition.  |
| sprob  | vector. Vector of posterior probabilities. If ng>1 the probabilities are weighted averaged over GAMMA.   |
| pgam   | vector. Vector of values of the unscaled posterior density of GAMMA.   |
| prob   | matrix. Matrix of marginal factor posterior probabilities for each of the different values of GAMMA.   |
| ind    | integer. Indicator variable. ind is 1 if the 'bm' subroutine exited properly. Any other number correspond to the format label number in the FORTRAN subroutine script. |

### Note

The function is a wrapper to call the FORTRAN subroutine 'bm', modification of Daniel Meyer's original program, 'mbcqp5.f', for the application of Bayesian design and analysis of fractional factorial experiments, part of the **mdopt** bundle, available at *StatLib*.

### Author(s)

R. Daniel Meyer. Adapted for R by Ernesto Barrios.



## References

- Box, G. E. P and R. D. Meyer (1986). "An Analysis for Unreplicated Fractional Factorials". *Technometrics*. Vol. 28. No. 1. pp. 11–18.
- Box, G. E. P and R. D. Meyer (1993). "Finding the Active Factors in Fractionated Screening Experiments". *Journal of Quality Technology*. Vol. 25. No. 2. pp. 94–105.

## See Also

[print.BsProb](#), [print.BsProb](#), [summary.BsProb](#).

## Examples

```
library(BsMD)
data(BM86.data,package="BsMD")
X <- as.matrix(BM86.data[,1:15])
y <- BM86.data["y1"]
# Using prior probability of p = 0.20, and k = 10 (gamma = 2.49)
drillAdvance.BsProb <- BsProb(X = X, y = y, blk = 0, mFac = 15, mInt = 1,
                             p = 0.20, g = 2.49, ng = 1, nMod = 10)
plot(drillAdvance.BsProb)
summary(drillAdvance.BsProb)

# Using prior probability of p = 0.20, and a 5 <= k <= 15 (1.22 <= gamma <= 3.74)
drillAdvance.BsProbG <- BsProb(X = X, y = y, blk = 0, mFac = 15, mInt = 1,
                              p = 0.25, g = c(1.22, 3.74), ng = 3, nMod = 10)
plot(drillAdvance.BsProbG, code = FALSE, prt = TRUE)
```

---

DanielPlot

*Normal Plot of Effects*

---

## Description

Normal plot of effects from a two level factorial experiment.

## Usage

```
DanielPlot(fit, code = FALSE, faclab = NULL, block = FALSE,
           datax = TRUE, half = FALSE, pch = "*", cex.fac = par("cex.lab"),
           cex.lab = par("cex.lab"), cex.pch = par("cex.axis"), ...)
```

## Arguments

- |                     |  |
|---------------------|--|
| <code>fit</code>    | object of class <code>lm</code> . Fitted model from <code>lm</code> or <code>aov</code> .  |
| <code>code</code>   | logical. If <code>TRUE</code> labels "A", "B", etc are used instead of the names of the coefficients (factors).  |
| <code>faclab</code> | list. If <code>NULL</code> points are labelled accordingly to <code>code</code> , otherwise <code>faclab</code> should be a list with <code>idx</code> (integer vector) and <code>lab</code> (character vector) components. See Details. |

|         |   |
|---------|---|
| block   | logical. If TRUE, the first factor is labelled as "BK" (block).   |
| datax   | logical. If TRUE, the x-axis is used for the factor effects the the y-axis for the normal scores. The opposite otherwise. |
| half    | logical. If TRUE, half-normal plot of effects is display.   |
| pch     | numeric or character. Points character.   |
| cex.fac | numeric. Factors' labels character size.  |
| cex.lab | numeric. Labels character size.   |
| cex.pch | numeric. Points character size.   |
| ...     | graphical parameters passed to plot.  |

### Details

The two levels design are assumed -1 and 1. Factor effects assumed  $2 \times \text{coef}(\text{obj})$  ((Intercept) removed) are displayed in a qqnorm plot with the effects in the x-axis by default. If half=TRUE the half-normal plots of effects is plotted as the normal quantiles of  $0.5 \times (\text{rank}(\text{abs}(\text{effects})) - 0.5) / \text{length}(\text{effects}) + 1$  versus  $\text{abs}(\text{effects})$ .

### Value

The function returns invisible data frame with columns: x, y and no, for the coordinates and the enumeration of plotted points. Names of the factor effects (coefficients) are the row names of the data frame.

### Author(s)

Ernesto Barrios.

### References

- C. Daniel (1976). *Application of Statistics to Industrial Experimentation*. Wiley.  
 Box G. E. P, Hunter, W. C. and Hunter, J. S. (1978). *Statistics for Experimenters*. Wiley.

### See Also

[qqnorm](#), [LenthPlot](#)

### Examples

```
### Injection Molding Experiment. Box et al. 1978.
library(BsMD)
# Data
data(BM86.data, package="BsMD") # Design matrix and response
print(BM86.data) # from Box and Meyer (1986)

# Model Fitting. Box and Meyer (1986) example 3.
injectionMolding.lm <- lm(y3 ~ X1 + X2 + X3 + X4 + X5 + X6 + X7 + X8 + X9 +
  X10 + X11 + X12 + X13 + X14 + X15, data = BM86.data)
print(coef(injectionMolding.lm)) # Model coefficients
```

```
# Daniel Plots
par(mfrow=c(1,3),oma=c(0,0,1,0),pty="s")
DanielPlot(injectionMolding.lm, half = TRUE, main = "Half-Normal Plot")
DanielPlot(injectionMolding.lm, main = "Normal Plot of Effects")
DanielPlot(injectionMolding.lm,
           faclab = list(idx = c(12,4,13), lab = c(" -H", " VG", " -B")),
           main = "Active Contrasts")
```

LenthPlot

*Lenth's Plot of Effects***Description**

Plot of the factor effects with significance levels based on robust estimation of contrast standard errors.

**Usage**

```
LenthPlot(obj, alpha = 0.05, plt = TRUE, limits = TRUE,
          xlab = "factors", ylab = "effects", faclab = NULL, cex.fac = par("cex.lab"),
          cex.axis=par("cex.axis"), adj = 1, ...)
```

**Arguments**

|          |   |
|----------|---|
| obj      | object of class <code>lm</code> or vector with the factor effects.  |
| alpha    | numeric. Significance level used for the <i>margin of error</i> (ME) and <i>simultaneous margin of error</i> (SME). See Lenth(1989).  |
| plt      | logical. If TRUE, a spikes plot with the factor effects is displayed. Otherwise, no plot is produced.   |
| limits   | logical. If TRUE ME and SME limits are displayed and labeled.   |
| xlab     | character string. Used to label the x-axis. "factors" as default.   |
| ylab     | character string. Used to label the y-axis. "effects" as default.   |
| faclab   | list with components <code>idx</code> (numeric vector) and <code>lab</code> (character vector). The <code>idx</code> entries of effects vector (taken from <code>obj</code> ) are labelled as <code>lab</code> . The rest of the effect names are blanked. If NULL all factors are labelled using the coefficients' name. |
| cex.fac  | numeric. Character size used for the factor labels.   |
| cex.axis | numeric. Character size used for the axis.  |
| adj      | numeric between 0 and 1. Determines where to place the "ME" (margin of error) and the "SME" (simultaneous margin of error) labels (character size of $0.9 * \text{cex.axis}$ ). 0 for extreme left hand side, 1 for extreme right hand side.  |
| ...      | extra parameters passed to <code>plot</code> .  |

## Details

If `obj` is of class `lm`, `2*coef(obj)` is used as factor effect with the intercept term removed. Otherwise, `obj` should be a vector with the factor effects. Robust estimate of the contrasts standard error is used to calculate *marginal* (ME) and *simultaneous margin of error* (SME) for the provided significance  $(1 - \alpha)$  level. See Lenth(1989). Spikes are used to display the factor effects. If `faclab` is `NULL`, factors are labelled with the effects or coefficient names. Otherwise, those `faclab\${idx}` factors are labelled as `faclab\${lab}`. The rest of the factors are blanked.

## Value

The function is called mainly for its side effect. It returns a vector with the value of `alpha` used, the estimated PSE, ME and SME.

## Author(s)

Ernesto Barrios. Extension provided by Kjetil Kjernsmo (2013).

## References

Lenth, R. V. (1989). "Quick and Easy Analysis of Unreplicated Factorials". *Technometrics* Vol. 31, No. 4. pp. 469–473.

## See Also

[DanielPlot](#), [BsProb](#) and [plot.BsProb](#)

## Examples

```
### Tensile Strength Experiment. Taguchi and Wu. 1980
library(BsMD)
# Data
data(BM86.data,package="BsMD") # Design matrix and responses
print(BM86.data) # from Box and Meyer (1986)

# Model Fitting. Box and Meyer (1986) example 2.
tensileStrength.lm <- lm(y2 ~ X1 + X2 + X3 + X4 + X5 + X6 + X7 + X8 + X9 +
                        X10 + X11 + X12 + X13 + X14 + X15, data = BM86.data)
print(coef(tensileStrength.lm)) # Model coefficients

par(mfrow=c(1,2),pty="s")
DanielPlot(tensileStrength.lm, main = "Daniel Plot")
LenthPlot(tensileStrength.lm, main = "Lenth's Plot")
```

**Description**

Best follow-up experiments based on the MD criterion are suggested to discriminate between competing models.

**Usage**

MD(X, y, nFac, nBlk = 0, mInt = 3, g = 2, nMod, p, s2, nf, facts, nFDes = 4, Xcand, mIter = 20, nStart = 5, startDes = NULL, top = 20, eps = 1e-05)

**Arguments**

|          |   |
|----------|---|
| X        | matrix. Design matrix of the initial experiment.  |
| y        | vector. Response vector of the initial experiment.  |
| nFac     | integer. Number of factors in the initial experiment.   |
| nBlk     | integer $\geq 1$ . The number of blocking factors in the initial experiment. They are accommodated in the first columns of matrix X.  |
| mInt     | integer. Maximum order of the interactions in the models.   |
| g        | vector. Variance inflation factor for main effects (g[1]) and interactions effects (g[2]). If vector length is 1 the same inflation factor is used for main and interactions effects. |
| nMod     | integer. Number of competing models.  |
| p        | vector. Posterior probabilities of the competing models.  |
| s2       | vector. Competing model variances.  |
| nf       | vector. Factors considered in each of the models.   |
| facts    | matrix. Matrix [nMod x max(nf)] of factor numbers in the design matrix.   |
| nFDes    | integer. Number of runs to consider in the follow-up experiment.  |
| Xcand    | matrix. Candidate runs to be chosen for the follow-up design.   |
| mIter    | integer. If 0, then user-entered designs startDes are evaluated, otherwise the maximum number of iterations for each Wynn search.   |
| nStart   | integer. Number of starting designs.  |
| startDes | matrix. Matrix [nStart x nFDes]. Each row has the row numbers of the user-supplied starting design.   |
| top      | integer. Highest MD follow-up designs recorded.   |
| eps      | numeric. A small number (1e-5 by default) used for computations.  |

## Details

The MD criterion, proposed by Meyer, Steinberg and Box is used to discriminate among competing models. Random starting runs chosen from `Xcand` are used for the Wynn search of best MD follow-up designs. `nStart` starting points are tried in the search limited to `mIter` iterations. If `mIter=0` then `startDes` user-provided designs are used. Posterior probabilities and variances of the competing models are obtained from `BsProb`. The function calls the FORTRAN subroutine 'md' and captures summary results. The complete output of the FORTRAN code is save in the 'MDPrint.out' file in the working directory.

## Value

A list with all input and output parameters of the FORTRAN subroutine MD. Most of the variable names kept to match FORTRAN code.

|                      |  |
|----------------------|--|
| <code>NSTART</code>  | Number of starting designs.  |
| <code>NRUNS</code>   | Number of runs used in follow-up designs.  |
| <code>ITMAX</code>   | Maximum number of iterations for each Wynn search.   |
| <code>INITDES</code> | Number of starting points.   |
| <code>NO</code>      | Numbers of runs already completed before follow-up.  |
| <code>IND</code>     | Indicator; 0 indicates the user supplied starting designs.   |
| <code>X</code>       | Matrix for initial data ( <code>nrow(X)=N0</code> ; <code>ncol(X)=COLS+BL</code> ).  |
| <code>Y</code>       | Response values from initial experiment ( <code>length(Y)=N0</code> ).   |
| <code>GAMMA</code>   | Variance inflation factor.   |
| <code>GAM2</code>    | If <code>IND=1</code> , <code>GAM2</code> was used for interaction factors.  |
| <code>BL</code>      | Number of blocks ( $\geq 1$ ) accommodated in first columns of <code>X</code> and <code>Xcand</code>   |
| .                    | .  |
| <code>COLS</code>    | Number of factors.   |
| <code>N</code>       | Number of candidate runs.  |
| <code>Xcand</code>   | Matrix of candidate runs. ( <code>nrow(Xcand)=N</code> , <code>ncol(Xcand)=ncol(X)</code> ).   |
| <code>NM</code>      | Number of models considered.   |
| <code>P</code>       | Models posterior probability.  |
| <code>SIGMA2</code>  | Models variances.  |
| <code>NF</code>      | Number of factors per model.   |
| <code>MNF</code>     | Maximum number of factor in models. ( <code>MNF=max(NF)</code> ).  |
| <code>JFAC</code>    | Matrix with the factor numbers for each of the models.   |
| <code>CUT</code>     | Maximum interaction order considered.  |
| <code>MBEST</code>   | If <code>INITDES=0</code> , the first row of the <code>MBEST[1, ]</code> matrix has the first user-supplied starting design. The last row the <code>NSTART</code> -th user-supplied starting design. |
| <code>NTOP</code>    | Number of the top best designs.  |
| <code>TOPD</code>    | The D value for the best <code>NTOP</code> designs.  |
| <code>TOPDES</code>  | Top <code>NTOP</code> design factors.  |
| <code>ESP</code>     | "Small number" provided to the 'md' FORTRAN subroutine. $1e-5$ by default.   |
| <code>flag</code>    | Indicator = 1, if the 'md' subroutine finished properly, -1 otherwise.   |

**Note**

The function is a wrapper to call the FORTRAN subroutine ‘md’, modification of Daniel Meyer’s original program, ‘MD.f’, part of the **mdopt** bundle for Bayesian model discrimination of multifactor experiments.

**Author(s)**

R. Daniel Meyer. Adapted for R by Ernesto Barrios.

**References**

Meyer, R. D., Steinberg, D. M. and Box, G. E. P. (1996). "Follow-Up Designs to Resolve Confounding in Multifactor Experiments (with discussion)". *Technometrics*, Vol. 38, No. 4, pp. 303–332.

Box, G. E. P and R. D. Meyer (1993). "Finding the Active Factors in Fractionated Screening Experiments". *Journal of Quality Technology*. Vol. 25. No. 2. pp. 94–105.

**See Also**

[print.MD](#), [BsProb](#)

**Examples**

```
### Injection Molding Experiment. Meyer et al. 1996, example 2.
library(BsMD)
data(BM93.e3.data,package="BsMD")
X <- as.matrix(BM93.e3.data[1:16,c(1,2,4,6,9)])
y <- BM93.e3.data[1:16,10]
p <- c(0.2356,0.2356,0.2356,0.2356,0.0566)
s2 <- c(0.5815,0.5815,0.5815,0.5815,0.4412)
nf <- c(3,3,3,3,4)
facs <- matrix(c(2,1,1,1,1,3,3,2,2,2,4,4,3,4,3,0,0,0,0,4),nrow=5,
  dimnames=list(1:5,c("f1","f2","f3","f4")))
nFDes <- 4
Xcand <- matrix(c(1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,
  -1,-1,-1,-1,1,1,1,1,-1,-1,-1,-1,1,1,1,1,
  -1,-1,1,1,-1,-1,1,1,-1,-1,1,1,-1,-1,1,1,
  -1,1,-1,1,-1,1,-1,1,-1,1,-1,1,-1,1,-1,1,
  -1,1,1,-1,1,-1,-1,1,-1,-1,1,-1,1,1,-1),
  nrow=16,dimnames=list(1:16,c("blk","f1","f2","f3","f4")))
)
injectionMolding.MD <- MD(X = X, y = y, nFac = 4, nBlk = 1, mInt = 3,
  g = 2, nMod = 5, p = p, s2 = s2, nf = nf, facs = facs,
  nFDes = 4, Xcand = Xcand, mIter = 20, nStart = 25, top = 10)
summary(injectionMolding.MD)

### Reactor Experiment. Meyer et al. 1996, example 3.
par(mfrow=c(1,2),pty="s")
data(Reactor.data,package="BsMD")
```

```

# Posterior probabilities based on first 8 runs
X <- as.matrix(cbind(blk = rep(-1,8), Reactor.data[c(25,2,19,12,13,22,7,32), 1:5]))
y <- Reactor.data[c(25,2,19,12,13,22,7,32), 6]
reactor8.BsProb <- BsProb(X = X, y = y, blk = 1, mFac = 5, mInt = 3,
  p = 0.25, g = 0.40, ng = 1, nMod = 32)
plot(reactor8.BsProb,prt=TRUE,,main="(8 runs)")

# MD optimal 4-run design
p <- reactor8.BsProb$ptop
s2 <- reactor8.BsProb$sigtop
nf <- reactor8.BsProb$nf top
facs <- reactor8.BsProb$j top
nFDes <- 4
Xcand <- as.matrix(cbind(blk = rep(+1,32), Reactor.data[,1:5]))
reactor.MD <- MD(X = X, y = y, nFac = 5, nBlk = 1, mInt = 3, g = 0.40, nMod = 32,
  p = p, s2 = s2, nf = nf, facs = facs, nFDes = 4, Xcand = Xcand,
  mIter = 20, nStart = 25, top = 5)
summary(reactor.MD)

# Posterior probabilities based on all 12 runs
X <- rbind(X, Xcand[c(4,10,11,26), ])
y <- c(y, Reactor.data[c(4,10,11,26),6])
reactor12.BsProb <- BsProb(X = X, y = y, blk = 1, mFac = 5, mInt = 3,
  p = 0.25, g = 1.20, ng = 1, nMod = 5)
plot(reactor12.BsProb,prt=TRUE,main="(12 runs)")

```

---

PB12Des

*12-run Plackett-Burman Design Matrix*


---

## Description

12-run Plackett-Burman design matrix.

## Usage

```
data(PB12Des)
```

## Format

A data frame with 12 observations on the following 11 variables.

- x1** numeric vectors. Contrast factor.
- x2** numeric vectors. Contrast factor.
- x3** numeric vectors. Contrast factor.
- x4** numeric vectors. Contrast factor.
- x5** numeric vectors. Contrast factor.
- x6** numeric vectors. Contrast factor.
- x7** numeric vectors. Contrast factor.



**x8** numeric vectors. Contrast factor.  
**x9** numeric vectors. Contrast factor.  
**x10** numeric vectors. Contrast factor.  
**x11** numeric vectors. Contrast factor.

### Source

Box G. E. P, Hunter, W. C. and Hunter, J. S. (2004). *Statistics for Experimenters II*. Wiley.

### Examples

```
library(BsMD)
data(PB12Des, package="BsMD")
str(PB12Des)
X <- as.matrix(PB12Des)
print(t(X)%*%X)
```

---

plot.BsProb

*Plotting of Posterior Probabilities from Bayesian Screening*

---

### Description

Method function for plotting marginal factor posterior probabilities for Bayesian screening.

### Usage

```
## S3 method for class 'BsProb'
plot(x, code = TRUE, prt = FALSE, cex.axis=par("cex.axis"), ...)
```

### Arguments

|                       |  |
|-----------------------|--|
| <code>x</code>        | list. List of class BsProb output from the <a href="#">BsProb</a> function.      |
| <code>code</code>     | logical. If TRUE coded factor names are used.                                    |
| <code>prt</code>      | logical. If TRUE, summary of the posterior probabilities calculation is printed. |
| <code>cex.axis</code> | Magnification used for the axis annotation. See <a href="#">par</a> .            |
| <code>...</code>      | additional graphical parameters passed to plot.                                  |

### Details

A spike plot, similar to barplots, is produced with a spike for each factor. Marginal posterior probabilities are used for the vertical axis. If `code=TRUE`, `X1`, `X2`, ... are used to label the factors otherwise the original factor names are used. If `prt=TRUE`, the [print.BsProb](#) function is called and the posterior probabilities are displayed. When [BsProb](#) is called for more than one value of gamma ( $g$ ), the spikes for each factor probability are overlapped to show the resulting range of each marginal probability.

**Value**

The function is called for its side effects. It returns an invisible NULL.

**Author(s)**

Ernesto Barrios.

**References**

Box, G. E. P and R. D. Meyer (1986). "An Analysis for Unreplicated Fractional Factorials". *Technometrics*. Vol. 28. No. 1. pp. 11–18.

Box, G. E. P and R. D. Meyer (1993). "Finding the Active Factors in Fractionated Screening Experiments". *Journal of Quality Technology*. Vol. 25. No. 2. pp. 94–105.

**See Also**

[BsProb](#), [print.BsProb](#), [summary.BsProb](#).

**Examples**

```
library(BsMD)
data(BM86.data,package="BsMD")
X <- as.matrix(BM86.data[,1:15])
y <- BM86.data["y1"]
# Using prior probability of p = 0.20, and k = 10 (gamma = 2.49)
drillAdvance.BsProb <- BsProb(X = X, y = y, blk = 0, mFac = 15, mInt = 1,
                             p = 0.20, g = 2.49, ng = 1, nMod = 10)
plot(drillAdvance.BsProb)
summary(drillAdvance.BsProb)

# Using prior probability of p = 0.20, and a 5 <= k <= 15 (1.22 <= gamma <= 3.74)
drillAdvance.BsProbG <- BsProb(X = X, y = y, blk = 0, mFac = 15, mInt = 1,
                              p = 0.25, g = c(1.22, 3.74), ng = 3, nMod = 10)
plot(drillAdvance.BsProbG, code = FALSE, prt = TRUE)
```

---

print.BsProb

*Printing Posterior Probabilities from Bayesian Screening*

---

**Description**

Printing method for lists of class BsProb. Prints the posterior probabilities of factors and models from the Bayesian screening procedure.

**Usage**

```
## S3 method for class 'BsProb'
print(x, X = TRUE, resp = TRUE, factors = TRUE, models = TRUE,
      nMod = 10, digits = 3, plt = FALSE, verbose = FALSE, ...)
```

**Arguments**

|         |  |
|---------|--|
| x       | list. Object of BsProb class, output from the <a href="#">BsProb</a> function. |
| X       | logical. If TRUE, the design matrix is printed.                                |
| resp    | logical. If TRUE, the response vector is printed.                              |
| factors | logical. Marginal posterior probabilities are printed if TRUE.                 |
| models  | logical. If TRUE models posterior probabilities are printed.                   |
| nMod    | integer. Number of the top ranked models to print.                             |
| digits  | integer. Significant digits to use for printing.                               |
| plt     | logical. Factor marginal probabilities are plotted if TRUE.                    |
| verbose | logical. If TRUE, the unclass-ed list x is displayed.                          |
| ...     | additional arguments passed to print function.                                 |

**Value**

The function prints out marginal factors and models posterior probabilities. Returns invisible list with the components:

|               |  |
|---------------|--|
| calc          | numeric vector with general calculation information.         |
| probabilities | Data frame with the marginal posterior factor probabilities. |
| models        | Data frame with model the posterior probabilities.           |

**Author(s)**

Ernesto Barrios.

**References**

Box, G. E. P and R. D. Meyer (1986). "An Analysis for Unreplicated Fractional Factorials". *Technometrics*. Vol. 28. No. 1. pp. 11–18.

Box, G. E. P and R. D. Meyer (1993). "Finding the Active Factors in Fractionated Screening Experiments". *Journal of Quality Technology*. Vol. 25. No. 2. pp. 94–105.

**See Also**

[BsProb](#), [summary.BsProb](#), [plot.BsProb](#).

**Examples**

```
library(BsMD)
data(BM86.data,package="BsMD")
X <- as.matrix(BM86.data[,1:15])
y <- BM86.data["y1"]
# Using prior probability of p = 0.20, and k = 10 (gamma = 2.49)
drillAdvance.BsProb <- BsProb(X = X, y = y, blk = 0, mFac = 15, mInt = 1,
                             p = 0.20, g = 2.49, ng = 1, nMod = 10)
print(drillAdvance.BsProb)
```

```

plot(drillAdvance.BsProb)

# Using prior probability of  $p = 0.20$ , and a  $5 \leq k \leq 15$  ( $1.22 \leq \gamma \leq 3.74$ )
drillAdvance.BsProbG <- BsProb(X = X, y = y, blk = 0, mFac = 15, mInt = 1,
                             p = 0.25, g = c(1.22, 3.74), ng = 3, nMod = 10)
print(drillAdvance.BsProbG, X = FALSE, resp = FALSE)
plot(drillAdvance.BsProbG)

```

---

print.MD

---

*Print Best MD Follow-Up Experiments*


---

### Description

Printing method for lists of class MD. Displays the best MD criterion set of runs and their MD for follow-up experiments.

### Usage

```

## S3 method for class 'MD'
print(x, X = FALSE, resp = FALSE, Xcand = TRUE, models = TRUE, nMod = x$nMod,
      digits = 3, verbose=FALSE, ...)

```

### Arguments

|         |   |
|---------|---|
| x       | list of class MD. Output list of the MD function.                   |
| X       | logical. If TRUE, the initial design matrix is printed.             |
| resp    | logical. If TRUE, the response vector of initial design is printed. |
| Xcand   | logical. Prints the candidate runs if TRUE.                         |
| models  | logical. Competing models are printed if TRUE.                      |
| nMod    | integer. Top models to print.                                       |
| digits  | integer. Significant digits to use in the print out.                |
| verbose | logical. If TRUE, the unclass-ed x is displayed.                    |
| ...     | additional arguments passed to print generic function.              |

### Value

The function is mainly called for its side effects. Prints out the selected components of the class MD objects, output of the MD function. For example the marginal factors and models posterior probabilities and the top MD follow-up experiments with their corresponding MD statistic. It returns invisible list with the components:

|           |  |
|-----------|--|
| calc      | Numeric vector with basic calculation information.                                       |
| models    | Data frame with the competing models posterior probabilities.                            |
| follow-up | Data frame with the runs for follow-up experiments and their corresponding MD statistic. |

**Author(s)**

Ernesto Barrios.

**References**

Meyer, R. D., Steinberg, D. M. and Box, G. E. P. (1996). "Follow-Up Designs to Resolve Confounding in Multifactor Experiments (with discussion)". *Technometrics*, Vol. 38, No. 4, pp. 303–332.

Box, G. E. P and R. D. Meyer (1993). "Finding the Active Factors in Fractionated Screening Experiments". *Journal of Quality Technology*. Vol. 25. No. 2. pp. 94–105.

**See Also**

[MD, BsProb](#)

**Examples**

```
# Injection Molding Experiment. Meyer et al. 1996. Example 2.
# MD for one extra experiment.
library(BsMD)
data(BM93.e3.data,package="BsMD")
X <- as.matrix(BM93.e3.data[1:16,c(1,2,4,6,9)])
y <- BM93.e3.data[1:16,10]
nBlk <- 1
nFac <- 4
mInt <- 3
g <- 2
nMod <- 5
p <- c(0.2356,0.2356,0.2356,0.2356,0.0566)
s2 <- c(0.5815,0.5815,0.5815,0.5815,0.4412)
nf <- c(3,3,3,3,4)
facs <- matrix(c(2,1,1,1,1,3,3,2,2,2,4,4,3,4,3,0,0,0,0,4),nrow=5,
  dimnames=list(1:5,c("f1","f2","f3","f4")))
nFDes <- 1
Xcand <- matrix(c(1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,
  -1,-1,-1,-1,1,1,1,1,-1,-1,-1,-1,1,1,1,1,
  -1,-1,1,1,-1,-1,1,1,-1,-1,1,1,-1,-1,1,1,
  -1,1,-1,1,-1,1,-1,1,-1,1,-1,1,-1,1,-1,1,
  -1,1,1,-1,1,-1,-1,1,1,-1,1,-1,1,1,-1),
  nrow=16,dimnames=list(1:16,c("blk","f1","f2","f3","f4")))
)
mIter <- 0
startDes <- matrix(c(9,11,12,15),nrow=4)
top <- 10
injectionMolding.MD <- MD(X=X,y=y,nFac=nFac,nBlk=nBlk,mInt=mInt,g=g,
  nMod=nMod,p=p,s2=s2,nf=nf,facs=facs,
  nFDes=nFDes,Xcand=Xcand,mIter=mIter,startDes=startDes,top=top)

print(injectionMolding.MD)
summary(injectionMolding.MD)
```

---

|              |                                |
|--------------|--------------------------------|
| Reactor.data | <i>Reactor Experiment Data</i> |
|--------------|--------------------------------|

---

**Description**

Data of the Reactor Experiment from Box, Hunter and Hunter (1978).

**Usage**

```
data(Reactor.data)
```

**Format**

A data frame with 32 observations on the following 6 variables.

**A** numeric vector. Feed rate factor.

**B** numeric vector. Catalyst factor.

**C** numeric vector. Agitation rate factor.

**D** numeric vector. Temperature factor.

**E** numeric vector. Concentration factor.

**y** numeric vector. Percentage reacted response.

**Source**

Box G. E. P, Hunter, W. C. and Hunter, J. S. (2004). *Statistics for Experimenters II*. Wiley.

Box G. E. P, Hunter, W. C. and Hunter, J. S. (1978). *Statistics for Experimenters*. Wiley.

**Examples**

```
library(BsMD)
data(Reactor.data, package="BsMD")
print(Reactor.data)
```

---

|                |   |
|----------------|---|
| summary.BsProb | <i>Summary of Posterior Probabilities from Bayesian Screening</i> |
|----------------|---|

---

**Description**

Reduced printing method for class BsProb lists. Prints posterior probabilities of factors and models from Bayesian screening procedure.

**Usage**

```
## S3 method for class 'BsProb'
summary(object, nMod = 10, digits = 3, ...)
```

**Arguments**

|        |  |
|--------|--|
| object | list. BsProb class list. Output list of <a href="#">BsProb</a> function. |
| nMod   | integer. Number of the top ranked models to print.                       |
| digits | integer. Significant digits to use.                                      |
| ...    | additional arguments passed to summary generic function.                 |

**Value**

The function prints out the marginal factors and models posterior probabilities. Returns invisible list with the components:

|               |  |
|---------------|--|
| calc          | Numeric vector with basic calculation information.           |
| probabilities | Data frame with the marginal posterior factor probabilities. |
| models        | Data frame with the models posterior probabilities.          |

**Author(s)**

Ernesto Barrios.

**References**

Box, G. E. P and R. D. Meyer (1986). "An Analysis for Unreplicated Fractional Factorials". *Technometrics*. Vol. 28. No. 1. pp. 11–18.

Box, G. E. P and R. D. Meyer (1993). "Finding the Active Factors in Fractionated Screening Experiments". *Journal of Quality Technology*. Vol. 25. No. 2. pp. 94–105.

**See Also**

[BsProb](#), [print.BsProb](#), [plot.BsProb](#).

**Examples**

```
library(BsMD)
data(BM86.data,package="BsMD")
X <- as.matrix(BM86.data[,1:15])
y <- BM86.data["y1"]
# Using prior probability of p = 0.20, and k = 10 (gamma = 2.49)
drillAdvance.BsProb <- BsProb(X = X, y = y, blk = 0, mFac = 15, mInt = 1,
                             p = 0.20, g = 2.49, ng = 1, nMod = 10)
plot(drillAdvance.BsProb)
summary(drillAdvance.BsProb)

# Using prior probability of p = 0.20, and a 5 <= k <= 15 (1.22 <= gamma <= 3.74)
drillAdvance.BsProbG <- BsProb(X = X, y = y, blk = 0, mFac = 15, mInt = 1,
                              p = 0.25, g = c(1.22, 3.74), ng = 3, nMod = 10)
plot(drillAdvance.BsProbG)
summary(drillAdvance.BsProbG)
```

---

summary.MD

*Summary of Best MD Follow-Up Experiments*

---

### Description

Reduced printing method for lists of class MD. Displays the best MD criterion set of runs and their MD for follow-up experiments.

### Usage

```
## S3 method for class 'MD'  
summary(object, digits = 3, verbose=FALSE, ...)
```

### Arguments

|         |  |
|---------|--|
| object  | list of MD class. Output list of MD function.            |
| digits  | integer. Significant digits to use in the print out.     |
| verbose | logical. If TRUE, the unclass-ed object is displayed.    |
| ...     | additional arguments passed to summary generic function. |

### Value

It prints out the marginal factors and models posterior probabilities and the top MD follow-up experiments with their corresponding MD statistic.

### Author(s)

Ernesto Barrios.

### References

Meyer, R. D., Steinberg, D. M. and Box, G. E. P. (1996). "Follow-Up Designs to Resolve Confounding in Multifactor Experiments (with discussion)". *Technometrics*, Vol. 38, No. 4, pp. 303–332.

Box, G. E. P and R. D. Meyer (1993). "Finding the Active Factors in Fractionated Screening Experiments". *Journal of Quality Technology*. Vol. 25. No. 2. pp. 94–105.

### See Also

[print.MD](#) and [MD](#)



**Examples**

```
### Reactor Experiment. Meyer et al. 1996, example 3.
library(BsMD)
data(Reactor.data,package="BsMD")

# Posterior probabilities based on first 8 runs
X <- as.matrix(cbind(blk = rep(-1,8), Reactor.data[c(25,2,19,12,13,22,7,32), 1:5]))
y <- Reactor.data[c(25,2,19,12,13,22,7,32), 6]
reactor.BsProb <- BsProb(X = X, y = y, blk = 1, mFac = 5, mInt = 3,
  p = 0.25, g = 0.40, ng = 1, nMod = 32)

# MD optimal 4-run design
p <- reactor.BsProb$ptop
s2 <- reactor.BsProb$sigtop
nf <- reactor.BsProb$nfstop
facs <- reactor.BsProb$jstop
nFDes <- 4
Xcand <- as.matrix(cbind(blk = rep(+1,32), Reactor.data[,1:5]))
reactor.MD <- MD(X = X, y = y, nFac = 5, nBlk = 1, mInt = 3, g = 0.40, nMod = 32,
  p = p, s2 = s2, nf = nf, facs = facs, nFDes = 4, Xcand = Xcand,
  mIter = 20, nStart = 25, top = 5)
print(reactor.MD)
summary(reactor.MD)
```

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