Package 'gss'

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Description

A data set collected by Centers for Disease Control and Prevention concerning AIDS patients who were infected with the HIV virus through blood transfusion.

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Usage

```
data(aids)
```

Format

A data frame containing 295 observations on the following variables.

incu Time from HIV infection to AIDS diagnosis.

infe Time from HIV infection to end of data collection (July 1986).

age Age at time of blood transfusion.

Source

Wang, M.-C. (1989), A semiparametric model for randomly truncated data. *Journal of the American Statistical Association*, **84**, 742–748.

bacteriuria

Treatment of Bacteriuria

Description

Bacteriuria patients were randomly assigned to two treatment groups. Weekly binary indicator of bacteriuria was recorded for every patient over 4 to 16 weeks. A total of 72 patients were represented in the data, with 36 each in the two treatment groups.

Usage

```
data(bacteriuria)
```

Format

A data frame containing 820 observations on the following variables.

id Identification of patients, a factor.

trt Treatments 1 or 2, a factor. time Weeks after randomization.

infect Binary indicator of bacteriuria (bacteria in urine).

Source

Joe, H. (1997), Multivariate Models and Dependence Concepts. London: Chapman and Hall.

References

Gu, C. and Ma, P. (2005), Generalized nonparametric mixed-effect models: computation and smoothing parameter selection. *Journal of Computational and Graphical Statistics*, **14**, 485–504.

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Buffalo Annual Snowfall

Description

Annual snowfall accumulations in Buffalo, NY from 1910 to 1973.

Usage

```
data(buffalo)
```

Format

A vector of 63 numerical values.

Source

Scott, D. W. (1985), Average shifted histograms: Effective nonparametric density estimators in several dimensions. *The Annals of Statistics*, **13**, 1024–1040.

cdsscden

Evaluating Conditional PDF, CDF, and Quantiles of Smoothing Spline Conditional Density Estimates

Description

Evaluate conditional pdf, cdf, and quantiles of f(y1|x,y2) for smoothing spline conditional density estimates f(y|x).

Usage

```
cdsscden(object, y, x, cond, int=NULL)
cpsscden(object, q, x, cond)
cqsscden(object, p, x, cond)
```

Arguments

object	Object of class "sscden" or "sscden1".
x	Data frame of x values on which conditional density $f(y1 x,y2)$ is to be evaluated.
У	Data frame or vector of y1 points on which conditional density $f(y1 x,y2)$ is to be evaluated.
cond	One row data frame of conditioning variables y2.
q	Vector of points on which cdf is to be evaluated.
р	Vector of probabilities for which quantiles are to be calculated.
int	Vector of normalizing constants.

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Details

The arguments x and y are of the same form as the argument newdata in predict.lm, but y in cdsscden can take a vector for 1-D y1.

cpsscden and cqsscden naturally only work for 1-D y1.

Value

cdsscden returns a list object with the following elements.

pdf Matrix or vector of conditional pdf f(y1|x,y2), with each column corresponding

to a distinct x value.

int Vector of normalizing constants.

cpsscden and cqsscden return a matrix or vector of conditional cdf or quantiles of f(y1|x,y2).

Note

If variables other than factors or numerical vectors are involved in y1, the normalizing constants can not be computed.

See Also

Fitting function sscden and dsscden.

cdsscopu	Evaluating 1-D Conditional PDF, CDF, and Quantiles of Copula Density Estimates
	stry Estimates

Description

Evaluate conditional pdf, cdf, and quantiles of copula density estimates.

Usage

```
cdsscopu(object, x, cond, pos=1, int=NULL)
cpsscopu(object, q, cond, pos=1)
cqsscopu(object, p, cond, pos=1)
```

Arguments

object	Object of class "sscopu".
X	Vector of points on which conditional pdf is to be evaluated.
cond	Value of conditioning variables.
pos	Position of variable of interest.
int	Normalizing constant.
q	Vector of points on which conditional cdf is to be evaluated.
р	Vector of probabilities for which conditional quantiles are to be calculated.

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Value

A vector of conditional pdf, cdf, or quantiles.

See Also

Fitting functions sscopu and sscopu2, and dsscopu.

cdssden	Evaluating Conditional PDF, CDF, and Quantiles of Smoothing Spline Density Estimates

Description

Evaluate conditional pdf, cdf, and quantiles for smoothing spline density estimates.

Usage

```
cdssden(object, x, cond, int=NULL)
cpssden(object, q, cond)
cqssden(object, p, cond)
```

Arguments

object	Object of class "ssden".
X	Data frame or vector of points on which conditional density is to be evaluated.
cond	One row data frame of conditioning variables.
int	Normalizing constant.
q	Vector of points on which conditional cdf is to be evaluated.
p	Vector of probabilities for which conditional quantiles are to be calculated.

Details

The argument x in cdssden is of the same form as the argument newdata in predict.lm, but can take a vector for 1-D conditional densities.

cpssden and cqssden naturally only work for 1-D conditional densities of a numerical variable.

Value

cdssden returns a list object with the following elements.

pdf Vector of conditional pdf. int Normalizing constant.

cpssden and cqssden return a vector of conditional cdf or quantiles.

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Note

If variables other than factors or numerical vectors are involved in x, the normalizing constant can not be computed.

See Also

Fitting function ssden and dssden.

clim

Average Temperatures During December 1980 Through February 1981

Description

Average temperatures at 690 weather stations during December 1980 through February 1981.

Usage

data(clim)

Format

A data frame containing 690 observations on the following variables.

temp Average temperature, in Celsius.

geog Geographic location (latitude,longitude), in degrees, as a matrix.

Source

This is reformulated from the data frame climate in the R package assist by Yuedong Wang and Chunlei Ke.

ColoCan

Colorectal Cancer Mortality Rate in Indiana Counties

Description

County-wise death counts of colorectal cancer patients in Indiana during years 2000 through 2004.

Usage

data(ColoCan)

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Format

A data frame containing 184 observations on the following variables.

```
event
        Death counts.
        Population from Census 2000.
pop
        Gender of population.
sex
        Proportion of Whites.
wrt
        Proportion of Blacks.
brt
ort
        Proportion of other minorities.
lat
        Latitude.
        Longitude.
lon
        Geographic location, derived from lat and lon.
geog
        Colorectal cancer screening rate.
scrn
name
        County name.
```

Details

geog was generated from lat and lon using the code given in the example section.

Source

Dr. Tonglin Zhang.

References

Zhang, T. and Lin, G. (2009), Cluster detection based on spatial associations and iterated residuals in generalized linear mixed models. *Biometrics*, **65**, 353–360.

Examples

```
## Converting latitude and longitude to x-y coordinates
## The 49th county is Marion, where Indianapolis is located.
## Not run: ltln2xy <- function(latlon,latlon0) {
    lat <- latlon[,1]*pi/180; lon <- latlon[,2]*pi/180
    lt0 <- latlon0[1]*pi/180; ln0 <- latlon0[2]*pi/180
    x <- cos(lt0)*sin(lon-ln0); y <- sin(lat-lt0)
    cbind(x,y)
}
data(ColoCan)
latlon <- as.matrix(ColoCan[,c("lat","lon")])
ltln2xy(latlon,latlon[49,])
## Clean up
rm(ltln2xy,ColoCan,latlon)
## End(Not run)</pre>
```

DiaRet 9

Description

Time to blindness of 197 diabetic retinopathy patients who received a laser treatment in one eye.

Usage

```
data(DiaRet)
```

Format

A data frame containing 197 observations on the following variables.

id	Patient ID.
time1	Follow-up time of left eye.
time2	Follow-up time of right eye.
status1	Censoring indicator of left eye.
status2	Censoring indicator of right eye.
trt1	Treatment indicator of left eye.
trt2	Treatment indicator of right eye.
type	Type of diabetes.
age	Age of patient at diagnosis.
time.t	Follow-up time of treated eye.
time.u	Follow-up time of untreated eye.
status.t	Censoring indicator of treated eye.
status.u	Censoring indicator of untreated eye.

Source

This is reformatted from the data frame diabetes in the R package timereg by Thomas H. Scheike.

References

Huster, W.J., Brookmeyer, R., and Self, S.G. (1989), Modelling paired survival data with covariates. *Biometrics*, **45**, 145–56.

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dsscden	Evaluating PDF, CDF, and Quantiles of Smoothing Spline Conditional Density Estimates

Description

Evaluate pdf, cdf, and quantiles for smoothing spline conditional density estimates.

Usage

```
dsscden(object, y, x)
psscden(object, q, x)
qsscden(object, p, x)
d.sscden(object, x, y)
d.sscden1(object, x, y, scale=TRUE)
```

Arguments

object	Object of class "sscden" or "sscden1".
X	Data frame of x values on which conditional density $f(y x)$ is to be evaluated.
У	Data frame or vector of points on which conditional density $f(y x)$ is to be evaluated.
q	Vector of points on which cdf is to be evaluated.
р	Vector of probabilities for which quantiles are to be calculated.
scale	Flag indicating whether to use approximate scaling without quadrature.

Details

The arguments x and y are of the same form as the argument newdata in predict.lm, but y in dsscden can take a vector for 1-D responses.

psscden and qsscden naturally only work for 1-D responses.

Value

A matrix or vector of pdf, cdf, or quantiles of f(y|x), with each column corresponding to a distinct x value.

See Also

Fitting function sscden and cdsscden.

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dsscopu

Evaluating Copula Density Estimates

Description

Evaluate copula density estimates.

Usage

```
dsscopu(object, x, copu=TRUE)
```

Arguments

object Object of class "sscopu".

x Vector or matrix of point(s) on which copula density is to be evaluated.

copu Flag indicating whether to apply copularization.

Value

A vector of copula density values.

See Also

Fitting functions sscopu and sscopu2.

dssden

Evaluating PDF, CDF, and Quantiles of Smoothing Spline Density Estimates

Description

Evaluate pdf, cdf, and quantiles for smoothing spline density estimates.

Usage

```
dssden(object, x)
pssden(object, q)
qssden(object, p)
d.ssden(object, x)
d.ssden1(object, x)
```

Arguments

object	Object of class "ssden".
x	Data frame or vector of points on which density is to be evaluated.
q	Vector of points on which cdf is to be evaluated.
р	Vector of probabilities for which quantiles are to be calculated.

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Details

The argument x in dssden is of the same form as the argument newdata in predict.lm, but can take a vector for 1-D densities.

pssden and qssden naturally only work for 1-D densities.

Value

A vector of pdf, cdf, or quantiles.

See Also

Fitting function ssden and cdssden.

esc

Embryonic Stem Cell from Mouse

Description

Data concerning mouse embryonic stem cell gene expression and transcription factor association strength.

Usage

data(esc)

Format

A data frame containing 1027 genes with the following variables.

y1	Gene expression after 4 days.
y2	Gene expression after 8 days.
у3	Gene expression after 14 days.
klf4	Score of TFAS with KLF4.
nanog	Score of TFAS with NANOG.
oct4	Score of TFAS with OCT4.
sox2	Score of TFAS with SOX2.
clusterID	Cluster identification.

References

Cai, J., Xie, D., Fan, Z., Chipperfield, H., Marden, J., Wong, W. H., and Zhong, S. (2010), Modeling co-expression across species for complex traits: insights to the difference of human and mouse embryonic stem cells. *PLoS Computational Biology*, **6**, e1000707.

Ouyang, Z., Zhou, Q., and Wong, W. H. (2009), chip-seq of transcription factors predicts absolute and differential gene expression in embryonic stem cells. *Proceedings of the National Academy of Sciences of USA*, **106**, 21521–21526.

eyetrack 13

eyetrack

Eyesight Fixation in Eyetracking Experiments

Description

Eyesight Fixation during some eyetracking experiments in liguistic studies.

Usage

```
data(eyetrack)
```

Format

A data frame containing 13891 observations on the following variables.

```
time Time, in ms.

color Binary indicator, 1 if eyesight fixed on target or color competitor, a factor.

object Binary indicator, 1 if eyesight fixed on target or object competitor, a factor.

id Identification of homogeneous sessions, a factor.

cnt Multiplicity count.
```

Source

Dr. Anouschka Foltz.

References

Gu, C. and Ma, P. (2011), Nonparametric regression with cross-classified responses. Manuscript.

fitted.ssanova

Fitted Values and Residuals from Smoothing Spline ANOVA Fits

Description

Methods for extracting fitted values and residuals from smoothing spline ANOVA fits.

```
## S3 method for class 'ssanova'
fitted(object, ...)
## S3 method for class 'ssanova'
residuals(object, ...)
## S3 method for class 'gssanova'
fitted(object, ...)
## S3 method for class 'gssanova'
residuals(object, type="working", ...)
```

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Arguments

object Object of class "ssanova" or "gssanova".

type Type of residuals desired, with two alternatives "working" (default) or "deviance".

... Ignored.

Details

The fitted values for "gssanova" objects are on the link scale, so are the "working" residuals.

gastric Gastric Cancer Data

Description

Survival of gastric cancer patients under chemotherapy and chemotherapy-radiotherapy combination.

Usage

```
data(gastric)
```

Format

A data frame containing 90 observations on the following variables.

futime Follow-up time, in days.
status Censoring status.
trt Factor indicating the treatments: 1 – chemothrapy, 2 – combination.

Source

Moreau, T., O'Quigley, J., and Mesbah, M. (1985), A global goodness-of-fit statistic for the proportional hazards model. *Applied Statistics*, **34**, 212-218.

gauss.quad 15

gauss.quad	Generating Gauss-Legendre Quadrature	

Description

Generate Gauss-Legendre quadratures using the FORTRAN routine gaussq.f found on NETLIB.

Usage

```
gauss.quad(size, interval)
```

Arguments

size Size of quadrature.
interval Interval to be covered.

Value

gauss. quad returns a list object with the following elements.

pt Quadrature nodes. wt Quadrature weights.

gssanova	Fitting Smoothing Spline ANOVA Models with Non-Gaussian Re-
	sponses

Description

Fit smoothing spline ANOVA models in non-Gaussian regression. The symbolic model specification via formula follows the same rules as in 1m and g1m.

```
gssanova(formula, family, type=NULL, data=list(), weights, subset,
    offset, na.action=na.omit, partial=NULL, alpha=NULL, nu=NULL,
    id.basis=NULL, nbasis=NULL, seed=NULL, random=NULL,
    skip.iter=FALSE)
```

Arguments

formula	Symbolic description of the model to be fit.
family	Description of the error distribution. Supported are exponential families "binomial", "poisson", "Gamma", "inverse.gaussian", and "nbinomial". Also supported are accelerated life model families "weibull", "lognorm", and "loglogis". Further more, proportional odds logistic regression "polr" for ordinal response is also supported.
type	List specifying the type of spline for each variable. See mkterm for details.
data	Optional data frame containing the variables in the model.
weights	Optional vector of weights to be used in the fitting process.
subset	Optional vector specifying a subset of observations to be used in the fitting process.
offset	Optional offset term with known parameter 1.
na.action	Function which indicates what should happen when the data contain NAs.
partial	Optional symbolic description of parametric terms in partial spline models.
alpha	Tuning parameter defining cross-validation; larger values yield smoother fits. Defaults are alpha=1 for family="binomial" and alpha=1.4 otherwise.
nu	Inverse scale parameter in accelerated life model families. Ignored for exponential families.
id.basis	Index designating selected "knots".
nbasis	Number of "knots" to be selected. Ignored when id.basis is supplied.
seed	Seed for reproducible random selection of "knots". Ignored when id.basis is supplied.
random	Input for parametric random effects in nonparametric mixed-effect models. See mkran for details.
skip.iter	Flag indicating whether to use initial values of theta and skip theta iteration. See ssanova for notes on skipping theta iteration.

Details

The model specification via formula is intuitive. For example, $y\sim x1*x2$ yields a model of the form

$$y = C + f_1(x1) + f_2(x2) + f_{12}(x1, x2) + e$$

with the terms denoted by "1", "x1", "x2", and "x1:x2".

The model terms are sums of unpenalized and penalized terms. Attached to every penalized term there is a smoothing parameter, and the model complexity is largely determined by the number of smoothing parameters.

Only one link is implemented for each family. It is the logit link for "binomial", and the log link for "poisson", and "Gamma". For "nbinomial", the working parameter is the logit of the probability p; see NegBinomial. For "weibull", "lognorm", and "loglogis", it is the location parameter for the log lifetime.

The selection of smoothing parameters is through direct cross-validation. The cross-validation score used for family="poisson" is taken from density estimation as in Gu and Wang (2003), and those used for other families are derived following the lines of Gu and Xiang (2001).

A subset of the observations are selected as "knots." Unless specified via id.basis or nbasis, the number of "knots" q is determined by $max(30, 10n^{2/9})$, which is appropriate for the default cubic splines for numerical vectors.

Value

gssanova returns a list object of class c("gssanova", "ssanova").

The method summary.gssanova can be used to obtain summaries of the fits. The method predict.ssanova can be used to evaluate the fits at arbitrary points along with standard errors, on the link scale. The method project.gssanova can be used to calculate the Kullback-Leibler projection for model selection. The methods residuals.gssanova and fitted.gssanova extract the respective traits from the fits.

Responses

For family="binomial", the response can be specified either as two columns of counts or as a column of sample proportions plus a column of total counts entered through the argument weights, as in glm.

For family="nbinomial", the response may be specified as two columns with the second being the known sizes, or simply as a single column with the common unknown size to be estimated through the maximum likelihood.

For family="weibull", "lognorm", or "loglogis", the response consists of three columns, with the first giving the follow-up time, the second the censoring status, and the third the left-truncation time. For data with no truncation, the third column can be omitted.

For family="polr", the response should be an ordered factor.

Note

For simpler models and moderate sample sizes, the exact solution of gssanova0 can be faster.

The results may vary from run to run. For consistency, specify id.basis or set seed.

In gss versions earlier than 1.0, gssanova was under the name gssanova1.

References

Gu, C. and Xiang, D. (2001), Cross validating non Gaussian data: generalized approximate cross validation revisited. *Journal of Computational and Graphical Statistics*, **10**, 581–591.

Gu, C. and Wang, J. (2003), Penalized likelihood density estimation: Direct cross-validation and scalable approximation. *Statistica Sinica*, **13**, 811–826.

Gu, C. (2013), Smoothing Spline ANOVA Models (2nd Ed). New York: Springer-Verlag.

Gu, C. (2014), Smoothing Spline ANOVA Models: R Package gss. *Journal of Statistical Software*, 58(5), 1-25. URL http://www.jstatsoft.org/v58/i05/.

Examples

```
## Fit a cubic smoothing spline logistic regression model
test <- function(x)</pre>
        \{.3*(1e6*(x^11*(1-x)^6)+1e4*(x^3*(1-x)^10))-2\}
x < -(0:100)/100
p < -1-1/(1+exp(test(x)))
y \leftarrow rbinom(x,3,p)
logit.fit <- gssanova(cbind(y,3-y)~x,family="binomial")</pre>
## The same fit
logit.fit1 <- gssanova(y/3~x,"binomial", weights=rep(3,101),</pre>
                        id.basis=logit.fit$id.basis)
## Obtain estimates and standard errors on a grid
est <- predict(logit.fit,data.frame(x=x),se=TRUE)</pre>
## Plot the fit and the Bayesian confidence intervals
plot(x,y/3,ylab="p")
lines(x,p,col=1)
lines(x,1-1/(1+exp(est\$fit)),col=2)
lines(x,1-1/(1+exp(est\$fit+1.96*est\$se)),col=3)
lines(x,1-1/(1+exp(est\$fit-1.96*est\$se)),col=3)
## Fit a mixed-effect logistic model
data(bacteriuria)
bact.fit <- gssanova(infect~trt+time,family="binomial",data=bacteriuria,</pre>
                      id.basis=(1:820)[bacteriuria$id%in%c(3,38)],random=~1|id)
## Predict fixed effects
predict(bact.fit,data.frame(time=2:16,trt=as.factor(rep(1,15))),se=TRUE)
## Estimated random effects
bact.fit$b
## Clean up
## Not run: rm(test,x,p,y,logit.fit,logit.fit1,est,bacteriuria,bact.fit)
dev.off()
## End(Not run)
```

gssanova0

Fitting Smoothing Spline ANOVA Models with Non-Gaussian Responses

Description

Fit smoothing spline ANOVA models in non-Gaussian regression. The symbolic model specification via formula follows the same rules as in 1m and g1m.

Arguments

formula Symbolic description of the model to be fit. family Description of the error distribution. Supported are exponential families "binomial", "poisson", "Gamma", "inverse.gaussian", and "nbinomial". Also supported are accelerated life model families "weibull", "lognorm", and "loglogis". Further more, proportional odds logistic regression "polr" for ordinal response is also supported. List specifying the type of spline for each variable. See mkterm for details. type data Optional data frame containing the variables in the model. Optional vector of weights to be used in the fitting process. weights Optional vector specifying a subset of observations to be used in the fitting prosubset cess. offset Optional offset term with known parameter 1. na.action Function which indicates what should happen when the data contain NAs. partial Optional symbolic description of parametric terms in partial spline models. method Score used to drive the performance-oriented iteration. Supported are method="v" for GCV, method="m" for GML, and method="u" for Mallows' CL. varht Dispersion parameter needed for method="u". Ignored when method="v" or method="m" are specified. Inverse scale parameter in accelerated life model families. Ignored for exponennu tial families. prec Precision requirement for the iterations. Maximum number of iterations allowed for performance-oriented iteration, and maxiter for inner-loop multiple smoothing parameter selection when applicable. alpha Tuning parameter modifying GCV or Mallows' CL. id.basis Index designating selected "knots". Number of "knots" to be selected. Ignored when id. basis is supplied. nbasis Seed for reproducible random selection of "knots". Ignored when id.basis is seed supplied. Input for parametric random effects in nonparametric mixed-effect models. See random mkran for details. skip.iter Flag indicating whether to use initial values of theta and skip theta iteration. See ssanova for notes on skipping theta iteration.

Details

The model specification via formula is intuitive. For example, y~x1*x2 yields a model of the form

$$y = C + f_1(x1) + f_2(x2) + f_{12}(x1, x2) + e$$

with the terms denoted by "1", "x1", "x2", and "x1:x2".

The model terms are sums of unpenalized and penalized terms. Attached to every penalized term there is a smoothing parameter, and the model complexity is largely determined by the number of smoothing parameters.

Only one link is implemented for each family. It is the logit link for "binomial", and the log link for "poisson", "Gamma", and "inverse.gaussian". For "nbinomial", the working parameter is the logit of the probability p; see NegBinomial. For "weibull", "lognorm", and "loglogis", it is the location parameter for the log lifetime.

The models are fitted by penalized likelihood method through the performance-oriented iteration as described in the reference. For family="binomial", "poisson", "nbinomial", "weibull", "lognorm", and "loglogis", the score driving the performance-oriented iteration defaults to method="u" with varht=1. For family="Gamma" and "inverse.gaussian", the default is method="v".

gssanova0 uses the algorithm of ssanova0 for the iterated penalized least squares problems, whereas gssanova1 uses the algorithm of ssanova.

In gssanova1, a subset of the observations are selected as "knots." Unless specified via id.basis or nbasis, the number of "knots" q is determined by $max(30, 10n^{2/9})$, which is appropriate for the default cubic splines for numerical vectors.

Value

gssanova0 returns a list object of class c("gssanova0", "ssanova0", "gssanova"). gssanova1 returns a list object of class c("gssanova", "ssanova").

The method summary.gssanova@ or summary.gssanova can be used to obtain summaries of the fits. The method predict.ssanova@ or predict.ssanova can be used to evaluate the fits at arbitrary points along with standard errors, on the link scale. The methods residuals.gssanova and fitted.gssanova extract the respective traits from the fits.

Responses

For family="binomial", the response can be specified either as two columns of counts or as a column of sample proportions plus a column of total counts entered through the argument weights, as in glm.

For family="nbinomial", the response may be specified as two columns with the second being the known sizes, or simply as a single column with the common unknown size to be estimated through the maximum likelihood.

For family="weibull", "lognorm", or "loglogis", the response consists of three columns, with the first giving the follow-up time, the second the censoring status, and the third the left-truncation time. For data with no truncation, the third column can be omitted.

For family="polr", the response should be an ordered factor.

Note

The direct cross-validation of gssanova can be more effective, and more stable for complex models.

For large sample sizes, the approximate solutions of gssanova1 and gssanova can be faster than gssanova0.

The results from gssanoval may vary from run to run. For consistency, specify id.basis or set seed

The method project is not implemented for gssanova0, nor is the mixed-effect model support through mkran.

In gss versions earlier than 1.0, gssanova@ was under the name gssanova.

References

Gu, C. (1992), Cross-validating non Gaussian data. *Journal of Computational and Graphical Statistics*, **1**, 169-179.

Gu, C. (2013), Smoothing Spline ANOVA Models (2nd Ed). New York: Springer-Verlag.

GU, C. (2014), Smoothing Spline ANOVA Models: R Package gss. *Journal of Statistical Software*, 58(5), 1-25. URL http://www.jstatsoft.org/v58/i05/.

Examples

```
## Fit a cubic smoothing spline logistic regression model
test <- function(x)</pre>
        \{.3*(1e6*(x^11*(1-x)^6)+1e4*(x^3*(1-x)^10))-2\}
x < -(0:100)/100
p <- 1-1/(1+exp(test(x)))
y \leftarrow rbinom(x,3,p)
logit.fit <- gssanova0(cbind(y,3-y)~x,family="binomial")</pre>
## The same fit
logit.fit1 \leftarrow gssanova0(y/3~x,"binomial",weights=rep(3,101))
## Obtain estimates and standard errors on a grid
est <- predict(logit.fit,data.frame(x=x),se=TRUE)</pre>
## Plot the fit and the Bayesian confidence intervals
plot(x,y/3,ylab="p")
lines(x,p,col=1)
lines(x,1-1/(1+exp(est\$fit)),col=2)
lines(x,1-1/(1+exp(est\$fit+1.96*est\$se)),col=3)
lines(x,1-1/(1+exp(est\$fit-1.96*est\$se)),col=3)
## Clean up
## Not run: rm(test,x,p,y,logit.fit,logit.fit1,est)
dev.off()
## End(Not run)
```

22 hzdrate.sshzd

hzdrate.sshzd	Evaluating Smoothing Spline Hazard Estimates	

Description

Evaluate smoothing spline hazard estimates by sshzd.

Usage

```
hzdrate.sshzd(object, x, se=FALSE, include=c(object$terms$labels,object$lab.p))
hzdcurve.sshzd(object, time, covariates=NULL, se=FALSE)
survexp.sshzd(object, time, covariates=NULL, start=0)
```

Arguments

object Object of class "sshzd".

x Data frame or vector of points on which hazard is to be evaluated.

se Flag indicating if standard errors are required.

include List of model terms to be included in the evaluation.

time Vector of time points.

covariates Vector of covariate values.

start Optional starting times of the intervals.

Value

For se=FALSE, hzdrate.sshzd returns a vector of hazard evaluations, and hzdcurve.sshzd returns a vector or columns of hazard curve(s) evaluated on time points at the covariates values. For se=TRUE, hzdrate.sshzd and hzdcurve.sshzd return a list consisting of the following elements.

fit Vector or columns of hazard.

se.fit Vector or columns of standard errors for log hazard.

survexp. sshzd returns a vector or columns of expected survivals based on the cumulative hazards over (start, time) at the covariates values, which in fact are the (conditional) survival probabilities S(time)/S(start).

Note

For left-truncated data, start must be at or after the earliest truncation point.

See Also

Fitting function sshzd.

hzdrate.sshzd2d 23

hzdrate.sshzd2d	Evaluating 2-D Smoothing Spline Hazard Estimates

Description

Evaluate 2-D smoothing spline hazard estimates by sshzd2d.

Usage

```
hzdrate.sshzd2d(object, time, covariates=NULL)
survexp.sshzd2d(object, time, covariates=NULL, job=3)
```

Arguments

object Object of class "sshzd2d".

time Matrix or vector of time points on which hazard or survival function is to be

evaluated.

covariates Data frame of covariate values.

job Flag indicating which survival function to evaluate.

Value

A vector of hazard or survival values.

Note

For job=1, 2, survexp. sshzd2d returns marginal survival S1(t) or S2(t). For job=3, survexp. sshzd2d returns the 2-D survival S(t1,t2).

For hzdrate.sshzd2d and survexp.sshzd2d with job=3, time should be a matrix of two columns. For survexp.sshzd2d with job=1,2, time should be a vector.

When covariates is present, its length should be either 1 or that of time.

See Also

Fitting function sshzd2d.

24 LakeAcidity

LakeAcidity

Water Acidity in Lakes

Description

Data extracted from the Eastern Lake Survey of 1984 conducted by the United States Environmental Protection Agency, concerning 112 lakes in the Blue Ridge.

Usage

```
data(LakeAcidity)
```

Format

A data frame containing 112 observations on the following variables.

ph Surface ph.
cal Calcium concentration.
lat Latitude.
lon Longitude.
geog Geographic location, derived from lat and lon

Details

geog was generated from lat and lon using the code given in the Example section.

Source

Douglas, A. and Delampady, M. (1990), Eastern Lake Survey – Phase I: Documentation for the Data Base and the Derived Data sets. Tech Report 160 (SIMS), Dept. Statistics, University of British Columbia.

References

Gu, C. and Wahba, G. (1993), Semiparametric analysis of variance with tensor product thin plate splines. *Journal of the Royal Statistical Society Ser. B*, **55**, 353–368.

Examples

```
## Converting latitude and longitude to x-y coordinates
## Not run: ltln2xy <- function(latlon,latlon0) {
    lat <- latlon[,1]*pi/180; lon <- latlon[,2]*pi/180
    lt0 <- latlon0[1]*pi/180; ln0 <- latlon0[2]*pi/180
    x <- cos(lt0)*sin(lon-ln0); y <- sin(lat-lt0)
    cbind(x,y)
}
data(LakeAcidity)
latlon <- as.matrix(LakeAcidity[,c("lat","lon")])
m.lat <- (min(latlon[,1])+max(latlon[,1]))/2</pre>
```

nlm0 25

```
m.lon <- (min(latlon[,2])+max(latlon[,2]))/2
ltln2xy(latlon,c(m.lat,m.lon))
## Clean up
rm(ltln2xy,LakeAcidity,latlon,m.lat,m.lon)
## End(Not run)</pre>
```

nlm0

Minimizing Univariate Functions on Finite Intervals

Description

Minimize univariate functions on finite intervals using 3-point quadratic fit, with golden-section safe-guard.

Usage

```
nlm0(fun, range, prec=1e-7)
```

Arguments

fun Function to be minimized.

range Interval on which the function to be minimized.

prec Desired precision of the solution.

Value

nlm0 returns a list object with the following elements.

estimate Minimizer. minimum Minimum.

evaluations Number of function evaluations.

NO2

Air Pollution and Road Traffic

Description

A subset of 500 hourly observations collected by the Norwegian Public Roads Administration at Alnabru in Oslo, Norway, between October 2001 and August 2003.

```
data(NO2)
```

26 nox

Format

A data frame containing 500 observations on the following variables.

no2 Concentration of NO2, on log scale.

cars Traffic volume of the hour, on log scale.

temp Temperature 2 meters above ground, in Celsius.

wind wind speed, meters/second.

temp2 Temperature difference between 25 and 2 meters above ground, in Celsius.

wind2 Wind direction, in degrees between 0 and 360.

Source

Statlib Datasets Archive at http://lib.stat.cmu.edu/datasets, contributed by Magne Aldrin.

nox NOx in Engine Exhaust

Description

Data from an experiment in which a single-cylinder engine was run with ethanol to see how the NOx concentration in the exhaust depended on the compression ratio and the equivalence ratio.

Usage

data(nox)

Format

A data frame containing 88 observations on the following variables.

nox NOx concentration in exhaust.
comp Compression ratio.
equi Equivalence ratio.

Source

Brinkman, N. D. (1981), Ethanol fuel – a single-cylinder engine study of efficiency and exhaust emissions. *SAE Transactions*, **90**, 1410–1424.

References

Cleveland, W. S. and Devlin, S. J. (1988), Locally weighted regression: An approach to regression analysis by local fitting. *Journal of the American Statistical Association*, **83**, 596–610.

Breiman, L. (1991), The pi method for estimating multivariate functions from noisy data. *Technometrics*, **33**, 125–160.

ozone 27

ozone

Ozone Concentration in Los Angeles Basin

Description

Daily measurements of ozone concentration and eight meteorological quantities in the Los Angeles basin for 330 days of 1976.

Usage

data(ozone)

Format

A data frame containing 330 observations on the following variables.

upo3	Upland ozone concentration, in ppm.
vdht	Vandenberg 500 millibar height, in meters.
wdsp	Wind speed, in miles per hour.
hmdt	Humidity.
sbtp	Sandburg Air Base temperature, in Celsius.
ibht	Inversion base height, in foot.
dgpg	Dagget pressure gradient, in mmHg.
ibtp	Inversion base temperature, in Fahrenheit.
vsty	Visibility, in miles.
dav	Calendar day, between 1 and 366.

Source

Unknown.

References

Breiman, L. and Friedman, J. H. (1985), Estimating optimal transformations for multiple regression and correlation. *Journal of the American Statistical Association*, **80**, 580–598.

Hastie, T. and Tibshirani, R. (1990), Generalized Additive Models. Chapman and Hall.

28 predict.ssanova

penny

Thickness of US Lincoln Pennies

Description

Thickness of US Lincoln pennies minted during years 1945 through 1989.

Usage

data(nox)

Format

A data frame containing 90 observations on the following variables.

year Year minted. mil Thickness in mils.

Source

Scott, D. W. (1992), *Multivariate Density Estimation: Theory, Practice and Visualization*. New York: Wiley.

References

Gu, C. (1995), Smoothing spline density estimation: Conditional distribution, *Statistica Sinica*, 5, 709–726.

Scott, D. W. (1992), Multivariate Density Estimation: Theory, Practice and Visualization. New York: Wiley.

predict.ssanova

Predicting from Smoothing Spline ANOVA Fits

Description

Evaluate terms in a smoothing spline ANOVA fit at arbitrary points. Standard errors of the terms can be requested for use in constructing Bayesian confidence intervals.

predict.ssanova 29

Usage

Arguments

object	Object of class inheriting from "ssanova".
newdata	Data frame or model frame in which to predict.
se.fit	Flag indicating if standard errors are required.
include	List of model terms to be included in the prediction. The offset term, if present, is to be specified by "offset".
contr	Contrast coefficients.
	Ignored.

Value

For se.fit=FALSE, predict.ssanova returns a vector of the evaluated fit.

For se.fit=TRUE, predict.ssanova returns a list consisting of the following elements.

fit Vector of evaluated fit.
se.fit Vector of standard errors.

Note

For mixed-effect models through ssanova or gssanova, the Z matrix is set to 0 if not supplied. To supply the Z matrix, add an element random=I(...) in newdata, where the as-is function I(...) preserves the integrity of the Z matrix in data frame.

predict1.ssanova takes a list of data frames in newdata representing x1, x2, etc. By default, it calculates f(x1)-f(x2) along with standard errors. While pairwise contrast is the targeted application, all linear combinations can be computed.

For "gssanova" objects, the results are on the link scale. See also predict9.gssanova.

References

Gu, C. (1992), Penalized likelihood regression: a Bayesian analysis. Statistica Sinica, 2, 255–264.

Gu, C. and Wahba, G. (1993), Smoothing spline ANOVA with component-wise Bayesian "confidence intervals." *Journal of Computational and Graphical Statistics*, **2**, 97–117.

Kim, Y.-J. and Gu, C. (2004), Smoothing spline Gaussian regression: more scalable computation via efficient approximation. *Journal of the Royal Statistical Society, Ser. B*, **66**, 337–356.

30 predict.sscox

See Also

Fitting functions ssanova, ssanova, gssanova, gssanova and methods summary.ssanova, summary.gssanova, summary.gssanova, fitted.ssanova.

Examples

```
## THE FOLLOWING EXAMPLE IS TIME-CONSUMING
## Not run:
## Fit a model with cubic and thin-plate marginals, where geog is 2-D
data(LakeAcidity)
fit <- ssanova(ph~log(cal)*geog,,LakeAcidity)</pre>
## Obtain estimates and standard errors on a grid
new <- data.frame(cal=1,geog=I(matrix(0,1,2)))</pre>
new <- model.frame(~log(cal)+geog,new)</pre>
predict(fit,new,se=TRUE)
## Evaluate the geog main effect
predict(fit,new,se=TRUE,inc="geog")
## Evaluate the sum of the geog main effect and the interaction
predict(fit,new,se=TRUE,inc=c("geog","log(cal):geog"))
## Evaluate the geog main effect on a grid
grid <- seq(-.04,.04,len=21)</pre>
new <- model.frame(~geog,list(geog=cbind(rep(grid,21),rep(grid,rep(21,21)))))</pre>
est <- predict(fit,new,se=TRUE,inc="geog")</pre>
## Plot the fit and standard error
par(pty="s")
contour(grid,grid,matrix(est$fit,21,21),col=1)
contour(grid,grid,matrix(est$se,21,21),add=TRUE,col=2)
## Clean up
rm(LakeAcidity,fit,new,grid,est)
dev.off()
## End(Not run)
```

predict.sscox

Evaluating Smoothing Spline ANOVA Estimate of Relative Risk

Description

Evaluate terms in a smoothing spline ANOVA estimate of relative risk at arbitrary points. Standard errors of the terms can be requested for use in constructing Bayesian confidence intervals.

predict.ssllrm 31

Arguments

object	Object of class "sscox".
newdata	Data frame or model frame in which to predict.
se.fit	Flag indicating if standard errors are required.
include	List of model terms to be included in the prediction.
	Ignored.

Value

For se.fit=FALSE, predict.sscox returns a vector of the evaluated relative risk. For se.fit=TRUE, predict.sscox returns a list consisting of the following elements.

fit Vector of evaluated relative risk.

se.fit Vector of standard errors for log relative risk.

Note

For mixed-effect models through sscox, the Z matrix is set to 0 if not supplied. To supply the Z matrix, add an element random=I(...) in newdata, where the as-is function I(...) preserves the integrity of the Z matrix in data frame.

See Also

Fitting functions sscox and method project.sscox.

predict.ssllrm Evaluating Log-Linear Regression Model Fits

Description

Evaluate conditional density in a log-linear regression model fit at arbitrary x, or contrast of log conditional density possibly with standard errors for constructing Bayesian confidence intervals.

Usage

```
## S3 method for class 'ssllrm'
predict(object, x, y=object$qd.pt, odds=NULL, se.odds=FALSE, ...)
```

Arguments

object	Object of class "ssllrm".
X	Data frame of x values.

y Data frame of y values; y-variables must be factors.

odds Optional coefficients of contrast.

se.odds Flag indicating if standard errors are required. Ignored when odds=NULL.

... Ignored.

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Value

For odds=NULL, predict.ssanova returns a vector/matrix of the estimated f(y|x).

When odds is given, it should match y in length and the coefficients must add to zero; predict.ssanova then returns a vector of estimated "odds ratios" if se.odds=FALSE or a list consisting of the following elements if se.odds=TRUE.

fit Vector of evaluated fit. se.fit Vector of standard errors.

See Also

Fitting function ssllrm.

Description

Evaluate smoothing spline ANOVA fits with non-Gaussian responses at arbitrary points, with results on the response scale.

Usage

```
## S3 method for class 'gssanova'
predict9(object, newdata, ci=FALSE, level=.95, nu=NULL, ...)
```

Arguments

object Object of class inheriting from "gssanova".

newdata Data frame or model frame in which to predict.

ci Flag indicating if Bayesian confidence intervals are required. Ignored for family="polr".

level Confidence level. Ignored when ci=FALSE.

nu Sizes for "nbinomial" fits with known sizes. Ignored otherwise.

... Ignored.

Value

For ci=FALSE, predict9.gssanova returns a vector of the evaluated fit,

For ci=TRUE, predict9.gssanova returns a list of three elements.

fit Vector of evaluated fit on response scale.

1c1 Vector of lower confidence limit on response scale.
uc1 Vector of upper confidence limit on response scale.

For family="polr", predict9.gssanova returns a matrix of probabilities with each row adding up to 1.

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Note

For mixed-effect models through gssanova or gssanova1, the Z matrix is set to 0 if not supplied. To supply the Z matrix, add an element random=I(...) in newdata, where the as-is function I(...) preserves the integrity of the Z matrix in data frame.

Unlike on the link scale, partial sums make no sense on the response scale, so all terms are forced in here.

References

Gu, C. (2013), Smoothing Spline ANOVA Models (2nd Ed). New York: Springer-Verlag.

See Also

Fitting functions gssanova, gssanova1 and methods predict.ssanova, summary.gssanova, project.gssanova, fitted.gssanova.

print

Print Functions for Smoothing Spline ANOVA Models

Description

Print functions for Smoothing Spline ANOVA models.

```
## S3 method for class 'ssanova'
print(x, ...)
## S3 method for class 'ssanova0'
print(x, ...)
## S3 method for class 'gssanova'
print(x, ...)
## S3 method for class 'ssden'
print(x, ...)
## S3 method for class 'sscden'
print(x, ...)
## S3 method for class 'sshzd'
print(x, ...)
## S3 method for class 'sscox'
print(x, ...)
## S3 method for class 'ssllrm'
print(x, ...)
## S3 method for class 'summary.ssanova'
print(x, digits=6, ...)
## S3 method for class 'summary.gssanova'
print(x, digits=6, ...)
## S3 method for class 'summary.gssanova0'
print(x, digits=6, ...)
```

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Arguments

```
x Object of class ssanova, summary.ssanova, summary.gssanova, or ssden.digits Number of significant digits to be printed in values.... Ignored.
```

See Also

```
ssanova, ssanova0, gssanova0, ssden, ssllrm, sshzd, summary.ssanova, summary.gssanova, summary.gssanova0.
```

project

Projecting Smoothing Spline ANOVA Fits for Model Diagnostics

Description

Calculate Kullback-Leibler projection of smoothing spline ANOVA fits for model diagnostics.

```
project(object, ...)
## S3 method for class 'ssanova'
project(object, include, ...)
## S3 method for class 'ssanova9'
project(object, include, ...)
## S3 method for class 'gssanova'
project(object, include, ...)
## S3 method for class 'ssden'
project(object, include, mesh=FALSE, ...)
## S3 method for class 'ssden1'
project(object, include, drop1=FALSE, ...)
## S3 method for class 'sscden'
project(object, include, ...)
## S3 method for class 'sscden1'
project(object, include, ...)
## S3 method for class 'sshzd'
project(object, include, mesh=FALSE, ...)
## S3 method for class 'sscox'
project(object, include, ...)
## S3 method for class 'sshzd1'
project(object, include, ...)
## S3 method for class 'ssllrm'
project(object, include, ...)
```

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Arguments

object Object of class "ssanova", "gssanova", "ssden", "ssden1", "sscden1",

"sshzd", "sshzd1", or "ssllrm".

... Additional arguments. Ignored in project.x.

include List of model terms to be included in the reduced model space. The partial

and offset terms, if present, are to be specified by "partial" and "offset",

respectively.

mesh Flag indicating whether to return evaluations of the projection.

drop1 If TRUE, calculate p<-length(include) projections with include[-i], i=1,...,p.

Details

The entropy KL(fit0,null) can be decomposed as the sum of KL(fit0,fit1) and KL(fit1,null), where fit0 is the fit to be projected, fit1 is the projection in the reduced model space, and null is the constant fit. The ratio KL(fit0,fit1)/KL(fit0,null) serves as a diagnostic of the feasibility of the reduced model.

For regression fits, smoothness safe-guard is used to prevent interpolation, and KL(fit0,fit1)+KL(fit1,null) may not match KL(fit0,null) perfectly.

For mixed-effect models from ssanova and gssanova, the estimated random effects are treated as offset.

Value

The functions return a list consisting of the following elements.

ratio KL(fit0,fit1)/KL(fit0,null); the smaller the value, the more feasible the reduced

model is.

kl KL(fit0,fit1).

For regression fits, the list also contains the following element.

check KL(fit0,fit1)/KL(fit0,null)+KL(fit1,null)/KL(fit0,null); a value closer to 1 is pre-

ferred.

For density and hazard fits, the list may contain the following optional element.

mesh The evaluations of the projection.

Note

project.ssden1, project.sscden1, and project.sshzd1 calculates square error projections.

References

Gu, C. (2004), Model diagnostics for smoothing spline ANOVA models. *The Canadian Journal of Statistics*, **32**, 347–358.

See Also

Fitting functions ssanova, gssanova, ssden, sshzd, and sshzd1.

36 smolyak

Sachs

Protein Expression in Human Immune System Cells

Description

Data concerning protein expression levels in human immune system cells under stimulations.

Usage

```
data(Sachs)
```

Format

A data frame containing 7466 cells, with flow cytometry measurements of 11 phosphorylated proteins and phospholipids, on the log10 scale of the original.

praf	Raf phosphorylated at S259.
pmek	Mek1/mek2 phosphorylated at S217/S221.
plcg	Phosphorylation of phospholipase $C - \gamma$ on Y783.
pip2	Phophatidylinositol 4,5-biphosphate.
pip3	Phophatidylinositol 3,4,5-triphosphate.
p44.42	Erk1/erk2 phosphorylated at T202/Y204.
pakts473	AKT phosphorylated at S473.
pka	Phosphorylation of of protein kinase A substrates on 3 sites.
pkc	Phosphorylation of of protein kinase C substrates on S660.
p38	Erk1/erk2 phosphorylated at T180/Y182.
pjnk	Erk1/erk2 phosphorylated at T183/Y185.

Source

Sachs, K., Perez, O., Pe'er, D., Lauffenburger, D. A., and Nolan, G. P. (2005), Causal protein-signaling networks derived from multiparameter single-cell data. *Science*, **308** (5732), 523–529.

smolyak

Generating Smolyak Cubature

Description

Generate delayed Smolyak cubatures using C routines modified from smolyak.c found in Knut Petras' SMOLPACK.

```
smolyak.quad(d, k)
smolyak.size(d, k)
```

Arguments

d Dimension of unit cube.k Depth of algorithm.

Value

smolyak. quad returns a list object with the following elements.

pt Quadrature nodes in rows of matrix.

wt Quadrature weights.

smolyak.size returns an integer.

ssanova

Fitting Smoothing Spline ANOVA Models

Description

Fit smoothing spline ANOVA models in Gaussian regression. The symbolic model specification via formula follows the same rules as in 1m.

Usage

Arguments

formula	Symbolic description of the model to be fit.	
type	List specifying the type of spline for each variable. See mkterm for details.	
data	Optional data frame containing the variables in the model.	
weights	Optional vector of weights to be used in the fitting process.	
subset	Optional vector specifying a subset of observations to be used in the fitting process.	
offset	Optional offset term with known parameter 1.	
na.action	Function which indicates what should happen when the data contain NAs.	
partial	Optional symbolic description of parametric terms in partial spline models.	
method	Method for smoothing parameter selection. Supported are method="v" for GCV, method="m" for GML (REML), and method="u" for Mallows' CL.	
alpha	Parameter modifying GCV or Mallows' CL; larger absolute values yield smoother fits; negative value invokes a stable and more accurate GCV/CL evaluation algorithm but may take two to five times as long. Ignored when method="m" are specified.	

varht	External variance estimate needed for method="u". Ignored when method="v" or method="m" are specified.
id.basis	Index designating selected "knots".
nbasis	Number of "knots" to be selected. Ignored when id.basis is supplied.
seed	Seed to be used for the random generation of "knots". Ignored when id.basis is supplied.
random	Input for parametric random effects in nonparametric mixed-effect models. See mkran for details.
skip.iter	Flag indicating whether to use initial values of theta and skip theta iteration. See notes on skipping theta iteration.

Details

The model specification via formula is intuitive. For example, y~x1*x2 yields a model of the form

$$y = C + f_1(x1) + f_2(x2) + f_{12}(x1, x2) + e$$

with the terms denoted by "1", "x1", "x2", and "x1:x2".

The model terms are sums of unpenalized and penalized terms. Attached to every penalized term there is a smoothing parameter, and the model complexity is largely determined by the number of smoothing parameters.

A subset of the observations are selected as "knots." Unless specified via id.basis or nbasis, the number of "knots" q is determined by $max(30, 10n^{2/9})$, which is appropriate for the default cubic splines for numerical vectors.

Using q "knots," ssanova calculates an approximate solution to the penalized least squares problem using algorithms of the order $O(nq^2)$, which for q << n scale better than the $O(n^3)$ algorithms of ssanova0. For the exact solution, one may set q=n in ssanova, but ssanova0 would be much faster.

Value

ssanova returns a list object of class "ssanova".

The method summary.ssanova can be used to obtain summaries of the fits. The method predict.ssanova can be used to evaluate the fits at arbitrary points along with standard errors. The method project.ssanova can be used to calculate the Kullback-Leibler projection for model selection. The methods residuals.ssanova and fitted.ssanova extract the respective traits from the fits.

Skipping Theta Iteration

For the selection of multiple smoothing parameters, nlm is used to minimize the selection criterion such as the GCV score. When the number of smoothing parameters is large, the process can be time-consuming due to the great amount of function evaluations involved.

The starting values for the nlm iteration are obtained using Algorith 3.2 in Gu and Wahba (1991). These starting values usually yield good estimates themselves, leaving the subsequent quasi-Newton iteration to pick up the "last 10%" performance with extra effort many times of the initial one. Thus, it is often a good idea to skip the iteration by specifying skip.iter=TRUE, especially in high-dimensions and/or with multi-way interactions.

skip.iter=TRUE could be made the default in future releases.

Note

To use GCV and Mallows' CL unmodified, set alpha=1.

For simpler models and moderate sample sizes, the exact solution of ssanova0 can be faster.

The results may vary from run to run. For consistency, specify id.basis or set seed.

In gss versions earlier than 1.0, ssanova was under the name ssanova1.

References

Wahba, G. (1990), Spline Models for Observational Data. Philadelphia: SIAM.

Gu, C. and Wahba, G. (1991), Minimizing GCV/GML scores with multiple smoothing parameters via the Newton method. *SIAM Journal on Scientific and Statistical Computing*, **12**, 383–398.

Kim, Y.-J. and Gu, C. (2004), Smoothing spline Gaussian regression: more scalable computation via efficient approximation. *Journal of the Royal Statistical Society, Ser. B*, **66**, 337–356.

Gu, C. (2013), Smoothing Spline ANOVA Models (2nd Ed). New York: Springer-Verlag.

Gu, C. (2014), Smoothing Spline ANOVA Models: R Package gss. *Journal of Statistical Software*, 58(5), 1-25. URL http://www.jstatsoft.org/v58/i05/.

Examples

```
## Fit a cubic spline
x <- runif(100); y <- 5 + 3*sin(2*pi*x) + rnorm(x)
cubic.fit <- ssanova(y~x)</pre>
## Obtain estimates and standard errors on a grid
new <- data.frame(x=seq(min(x),max(x),len=50))</pre>
est <- predict(cubic.fit,new,se=TRUE)</pre>
## Plot the fit and the Bayesian confidence intervals
plot(x,y,col=1); lines(new$x,est$fit,col=2)
lines(new$x,est$fit+1.96*est$se,col=3)
lines(new$x,est$fit-1.96*est$se,col=3)
## Clean up
## Not run: rm(x,y,cubic.fit,new,est)
dev.off()
## End(Not run)
## Fit a tensor product cubic spline
data(nox)
nox.fit <- ssanova(log10(nox)~comp*equi,data=nox)</pre>
## Fit a spline with cubic and nominal marginals
nox$comp<-as.factor(nox$comp)</pre>
nox.fit.n <- ssanova(log10(nox)~comp*equi,data=nox)</pre>
## Fit a spline with cubic and ordinal marginals
nox$comp<-as.ordered(nox$comp)</pre>
nox.fit.o <- ssanova(log10(nox)~comp*equi,data=nox)</pre>
## Clean up
## Not run: rm(nox,nox.fit,nox.fit.n,nox.fit.o)
```

ssanova0 Fitting Smoothing Spline ANOVA Models	
--	--

Description

Fit smoothing spline ANOVA models in Gaussian regression. The symbolic model specification via formula follows the same rules as in 1m.

Usage

Arguments

formula	Symbolic description of the model to be fit.
type	List specifying the type of spline for each variable. See mkterm for details.
data	Optional data frame containing the variables in the model.
weights	Optional vector of weights to be used in the fitting process.
subset	Optional vector specifying a subset of observations to be used in the fitting process.
offset	Optional offset term with known parameter 1.
na.action	Function which indicates what should happen when the data contain NAs.
partial	Optional symbolic description of parametric terms in partial spline models.
method	Method for smoothing parameter selection. Supported are method="v" for GCV, method="m" for GML (REML), and method="u" for Mallow's CL.
varht	External variance estimate needed for method="u". Ignored when method="v" or method="m" are specified.
prec	Precision requirement in the iteration for multiple smoothing parameter selection. Ignored when only one smoothing parameter is involved.
maxiter	Maximum number of iterations allowed for multiple smoothing parameter selection. Ignored when only one smoothing parameter is involved.

Details

The model specification via formula is intuitive. For example, y~x1*x2 yields a model of the form

$$y = C + f_1(x1) + f_2(x2) + f_{12}(x1, x2) + e$$

with the terms denoted by "1", "x1", "x2", and "x1:x2".

The model terms are sums of unpenalized and penalized terms. Attached to every penalized term there is a smoothing parameter, and the model complexity is largely determined by the number of smoothing parameters.

ssanova0 and the affiliated methods provide a front end to RKPACK, a collection of RATFOR routines for nonparametric regression via the penalized least squares. The algorithms implemented in RKPACK are of the order $O(n^3)$.

Value

ssanova@returns a list object of class c("ssanova@", "ssanova").

The method summary.ssanova@can be used to obtain summaries of the fits. The method predict.ssanova@can be used to evaluate the fits at arbitrary points along with standard errors. The methods residuals.ssanova and fitted.ssanova extract the respective traits from the fits.

Note

For complex models and large sample sizes, the approximate solution of ssanova can be faster.

The method project is not implemented for ssanova0, nor is the mixed-effect model support through mkran.

In gss versions earlier than 1.0, ssanova0 was under the name ssanova.

References

```
Wahba, G. (1990), Spline Models for Observational Data. Philadelphia: SIAM. Gu, C. (2013), Smoothing Spline ANOVA Models (2nd Ed). New York: Springer-Verlag. Gu, C. (2014), Smoothing Spline ANOVA Models: R Package gss. Journal of Statistical Software, 58(5), 1-25. URL http://www.jstatsoft.org/v58/i05/.
```

Examples

```
## Fit a cubic spline
x \leftarrow runif(100); y \leftarrow 5 + 3*sin(2*pi*x) + rnorm(x)
cubic.fit <- ssanova0(y~x,method="m")</pre>
## Obtain estimates and standard errors on a grid
new <- data.frame(x=seq(min(x),max(x),len=50))</pre>
est <- predict(cubic.fit,new,se=TRUE)</pre>
## Plot the fit and the Bayesian confidence intervals
plot(x,y,col=1); lines(new$x,est$fit,col=2)
lines(new$x,est$fit+1.96*est$se,col=3)
lines(new$x,est$fit-1.96*est$se,col=3)
## Clean up
## Not run: rm(x,y,cubic.fit,new,est)
dev.off()
## End(Not run)
## Fit a tensor product cubic spline
nox.fit <- ssanova0(log10(nox)~comp*equi,data=nox)</pre>
## Fit a spline with cubic and nominal marginals
nox$comp<-as.factor(nox$comp)</pre>
nox.fit.n <- ssanova0(log10(nox)~comp*equi,data=nox)</pre>
## Fit a spline with cubic and ordinal marginals
nox$comp<-as.ordered(nox$comp)</pre>
nox.fit.o <- ssanova0(log10(nox)~comp*equi,data=nox)</pre>
## Clean up
## Not run: rm(nox,nox.fit,nox.fit.n,nox.fit.o)
```

ssanova9	Fitting Smoothing Spline ANOVA Models with Correlated Data

Description

Fit smoothing spline ANOVA models with correlated Gaussian data. The symbolic model specification via formula follows the same rules as in 1m.

Usage

Arguments

formula	Symbolic description of the model to be fit.
type	List specifying the type of spline for each variable. See mkterm for details.
data	Optional data frame containing the variables in the model.
subset	Optional vector specifying a subset of observations to be used in the fitting process.
offset	Optional offset term with known parameter 1.
na.action	Function which indicates what should happen when the data contain NAs.
partial	Optional symbolic description of parametric terms in partial spline models.
method	Method for smoothing parameter selection. Supported are method="v" for V, method="m" for M , and method="u" for U ; see the reference for definitions of U , V , and M .
alpha	Parameter modifying V or U ; larger absolute values yield smoother fits. Ignored when $method="m"$ are specified.
varht	External variance estimate needed for method="u". Ignored when method="v" or method="m" are specified.
id.basis	Index designating selected "knots".
nbasis	Number of "knots" to be selected. Ignored when id.basis is supplied.
seed	Seed to be used for the random generation of "knots". Ignored when ${\tt id.basis}$ is supplied.
cov	Input for covariance functions. See mkcov for details.
skip.iter	Flag indicating whether to use initial values of theta and skip theta iteration. See notes on skipping theta iteration.
fit	ssanova9 fit with ARMA error.

Details

The model specification via formula is intuitive. For example, y~x1*x2 yields a model of the form

$$y = C + f_1(x1) + f_2(x2) + f_{12}(x1, x2) + e$$

with the terms denoted by "1", "x1", "x2", and "x1:x2".

The model terms are sums of unpenalized and penalized terms. Attached to every penalized term there is a smoothing parameter, and the model complexity is largely determined by the number of smoothing parameters.

A subset of the observations are selected as "knots." Unless specified via id.basis or nbasis, the number of "knots" q is determined by $max(30, 10n^{2/9})$, which is appropriate for the default cubic splines for numerical vectors.

Using q "knots," ssanova calculates an approximate solution to the penalized least squares problem using algorithms of the order $O(nq^2)$, which for q << n scale better than the $O(n^3)$ algorithms of ssanova0. For the exact solution, one may set q=n in ssanova, but ssanova0 would be much faster.

Value

ssanova9 returns a list object of class c("ssanova9", "ssanova").

The method summary.ssanova9 can be used to obtain summaries of the fits. The method predict.ssanova can be used to evaluate the fits at arbitrary points along with standard errors. The method project.ssanova9 can be used to calculate the Kullback-Leibler projection for model selection. The methods residuals.ssanova and fitted.ssanova extract the respective traits from the fits.

para.arma returns the fitted ARMA coefficients for cov=list("arma",c(p,q)) in the call to ssanova9.

Skipping Theta Iteration

For the selection of multiple smoothing parameters, nlm is used to minimize the selection criterion such as the GCV score. When the number of smoothing parameters is large, the process can be time-consuming due to the great amount of function evaluations involved.

The starting values for the nlm iteration are obtained using Algorith 3.2 in Gu and Wahba (1991). These starting values usually yield good estimates themselves, leaving the subsequent quasi-Newton iteration to pick up the "last 10%" performance with extra effort many times of the initial one. Thus, it is often a good idea to skip the iteration by specifying skip.iter=TRUE, especially in high-dimensions and/or with multi-way interactions.

skip.iter=TRUE could be made the default in future releases.

Note

The results may vary from run to run. For consistency, specify id.basis or set seed.

References

```
Han, C. and Gu, C. (2008), Optimal smoothing with correlated data, Sankhya, 70-A, 38–72. Gu, C. (2013), Smoothing Spline ANOVA Models (2nd Ed). New York: Springer-Verlag. Gu, C. (2014), Smoothing Spline ANOVA Models: R Package gss. Journal of Statistical Software, 58(5), 1-25. URL http://www.jstatsoft.org/v58/i05/.
```

Examples

```
x <- runif(100); y <- 5 + 3*sin(2*pi*x) + rnorm(x)
## independent fit
fit <- ssanova9(y~x,cov=list("known",diag(1,100)))
## AR(1) fit
fit <- ssanova9(y~x,cov=list("arma",c(1,0)))
para.arma(fit)
## MA(1) fit
e <- rnorm(101); e <- e[-1]-.5*e[-101]
x <- runif(100); y <- 5 + 3*sin(2*pi*x) + e
fit <- ssanova9(y~x,cov=list("arma",c(0,1)))
para.arma(fit)
## Clean up
## Not run: rm(x,y,e,fit)</pre>
```

sscden

Estimating Conditional Probability Density Using Smoothing Splines

Description

Estimate conditional probability densities using smoothing spline ANOVA models. The symbolic model specification via formula follows the same rules as in 1m.

Usage

```
sscden(formula, response, type=NULL, data=list(), weights, subset,
    na.action=na.omit, alpha=1.4, id.basis=NULL, nbasis=NULL,
    seed=NULL, ydomain=as.list(NULL), yquad=NULL, prec=1e-7,
    maxiter=30, skip.iter=FALSE)

sscden1(formula, response, type=NULL, data=list(), weights, subset,
    na.action=na.omit, alpha=1.4, id.basis=NULL, nbasis=NULL,
    seed=NULL, rho=list("xy"), ydomain=as.list(NULL), yquad=NULL,
    prec=1e-7, maxiter=30, skip.iter=FALSE)
```

Arguments

formula Symbolic description of the model to be fit.

response Formula listing response variables.

type List specifying the type of spline for each variable. See mkterm for details.

data	Optional data frame containing the variables in the model.
	•
weights	Optional vector of counts for duplicated data.
subset	Optional vector specifying a subset of observations to be used in the fitting process.
na.action	Function which indicates what should happen when the data contain NAs.
alpha	Parameter defining cross-validation scores for smoothing parameter selection.
id.basis	Index of observations to be used as "knots."
nbasis	Number of "knots" to be used. Ignored when id.basis is specified.
seed	Seed to be used for the random generation of "knots." Ignored when id.basis is specified.
ydomain	Data frame specifying marginal support of conditional density.
yquad	Quadrature for calculating integral on Y domain. Mandatory if response variables other than factors or numerical vectors are involved.
prec	Precision requirement for internal iterations.
maxiter	Maximum number of iterations allowed for internal iterations.

rho

Details

skip.iter

The model is specified via formula and response, where response lists the response variables. For example, sscden(~y*x,~y) prescribe a model of the form

ssanova for notes on skipping theta iteration.

rho function needed for sscden1.

Flag indicating whether to use initial values of theta and skip theta iteration. See

$$log f(y|x) = g_y(y) + g_{xy}(x,y) + C(x)$$

with the terms denoted by "y", "y:x"; the term(s) not involving response(s) are removed and the constant C(x) is determined by the fact that a conditional density integrates to one on the y axis. sscden1 does keep terms not involving response(s) during estimation, although those terms cancel out when one evaluates the estimated conditional density.

The model terms are sums of unpenalized and penalized terms. Attached to every penalized term there is a smoothing parameter, and the model complexity is largely determined by the number of smoothing parameters.

A subset of the observations are selected as "knots." Unless specified via id.basis or nbasis, the number of "knots" q is determined by $max(30, 10n^{2/9})$, which is appropriate for the default cubic splines for numerical vectors.

Value

sscden returns a list object of class "sscden". sscden1 returns a list object of class c("sscden1", "sscden"). dsscden and cdsscden can be used to evaluate the estimated conditional density f(y|x) and f(y|x,y|x); psscden, qsscden, cpsscden, and cqsscden can be used to evaluate conditional cdf and quantiles. The methods project.sscden or project.sscden1 can be used to calculate the Kullback-Leibler or square-error projections for model selection.

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Note

Default quadrature on the Y domain will be constructed for numerical vectors on a hyper cube, then outer product with factor levels will be taken if factors are involved. The sides of the hyper cube are specified by ydomain; for ydomain\$y missing, the default is $c(\min(y), \max(y)) + c(-1, 1) * (\max(y) - \min(y)) * .05$.

On a 1-D interval, the quadrature is the 200-point Gauss-Legendre formula returned from gauss. quad. For multiple numerical vectors, delayed Smolyak cubatures from smolyak. quad are used on cubes with the marginals properly transformed; see Gu and Wang (2003) for the marginal transformations.

The results may vary from run to run. For consistency, specify id.basis or set seed.

For reasonable execution time in high dimensions, set skip.iter=TRUE.

References

Gu, C. (1995), Smoothing spline density estimation: Conditional distribution. *Statistica Sinica*, **5**, 709–726. Springer-Verlag.

Gu, C. (2014), Smoothing Spline ANOVA Models: R Package gss. *Journal of Statistical Software*, 58(5), 1-25. URL http://www.jstatsoft.org/v58/i05/.

Examples

sscomp

Composition Estimation

Description

Estimate composition using multinomial counts.

Usage

```
sscomp(x,wt=rep(1,length(x)),alpha=1.4)
sscomp2(x,alpha=1.4)
```

Arguments

x Numerical vector or matrix of multinomial counts.

wt Numerical vector of integration weights.

alpha Parameter defining cross-validation score for smoothing parameter selection.

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Details

sscomp takes a vector x to estimate composition using density estimation on a nominal discrete domain; zero counts must be included in x to specify the domain. wt mimicking the shape of the unknown density could improve performance.

sscomp2 takes a matrix x, collapses columns to estimate a density using sscomp, then using that as wt in further sscomp calls to estimate composition for each column.

Value

sscomp returns a column of estimated probabilities. sscomp2 returns a matrix of estimated probabilities, matching the input x in dimensions.

References

Gu, C. (2020), Composition estimation via shrinkage. manuscript.

sscopu

Estimating Copula Density Using Smoothing Splines

Description

Estimate copula densities using tensor-product cubic splines.

Usage

```
sscopu(x, symmetry=FALSE, alpha=1.4, order=NULL, exclude=NULL,
    weights=NULL, id.basis=NULL, nbasis=NULL, seed=NULL,
    qdsz.depth=NULL, prec=1e-7, maxiter=30, skip.iter=dim(x)[2]!=2)
sscopu2(x, censoring=NULL, truncation=NULL, symmetry=FALSE, alpha=1.4,
    weights=NULL, id.basis=NULL, nbasis=NULL, seed=NULL, prec=1e-7,
    maxiter=30)
```

Arguments

Χ	Matrix of observations on unit cubes.
symmetry	Flag indicating whether to enforce symmetry, or invariance under coordinate permutation.
order	Highest order of interaction terms in log density. When NULL, it is set to $\dim(x)[2]$ internally.
exclude	Pair(s) of marginals whose interactions to be excluded in log density.
alpha	Parameter defining cross-validation score for smoothing parameter selection.
weights	Optional vector of bin-counts for histogram data.
id.basis	Index of observations to be used as "knots."

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nbasis Number of "knots" to be used. Ignored when id. basis is specified.

seed Seed to be used for the random generation of "knots." Ignored when id.basis

is specified.

qdsz.depth Depth to be used in smolyak.quad for the generation of quadrature.

prec Precision requirement for internal iterations.

maxiter Maximum number of iterations allowed for internal iterations.

skip.iter Flag indicating whether to use initial values of theta and skip theta iteration. See

ssanova for notes on skipping theta iteration.

censoring Optional censoring indicator.
truncation Optional truncation points.

Details

sscopu is essentially ssden applied to observations on unit cubes. Instead of variables in data frames, the data are entered as a numerical matrix, and model complexity is globally controlled by the highest order of interactions allowed in log density.

sscopu2 further restricts the domain to the unit square, but allows for possible censoring and truncation. With censoring==0,1,2,3, a data point (x1,x2) represents exact observation, [0,x1]xx2, x1x[0,x2], or [0,x1]x[0,x2]. With truncation point (t1,t2), the sample is taken from [0,t1]x[0,t2] instead of the unit square.

With symmetriy=TRUE, one may enforce the interchangeability of coordinates so that f(x1, x2) = f(x2, x1), say.

When (1,2) is a row in exclude, interaction terms involving coordinates 1 and 2 are excluded.

Value

sscopu and sscopu2 return a list object of class "sscopu". dsscopu can be used to evaluate the estimated copula density. A "copularization" process is applied to the estimated density by default so the resulting marginal densities are guaranteed to be uniform.

cdsscopu, cpsscopu, and cqsscopu can be used to evaluate 1-D conditional pdf, cdf, and quantiles.

Note

For reasonable execution time in higher dimensions, set skip.iter=TRUE in calls to sscopu.

When "Newton iteration diverges" in sscopu, try to use a larger qdsz.depth; the default values for dimensions 2, 3, 4, 5, 6+ are 24, 14, 12, 11, 10. To be sure a larger qdsz.depth indeed makes difference, verify the cubature size using smolyak.size.

The results may vary from run to run. For consistency, specify id.basis or set seed.

Author(s)

Chong Gu, <chong@stat.purdue.edu>

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References

Gu, C. (2013), *Smoothing Spline ANOVA Models (2nd Ed)*. New York: Springer-Verlag. Gu, C. (2015), Hazard estimation with bivariate survival data and copula density estimation. *Journal*

Examples

```
## simulate 2-D data
x <- matrix(runif(200),100,2)
## fit copula density
fit <- sscopu(x)
## "same fit"
fit2 <- sscopu2(x,id=fit$id)
## symmetric fit
fit.s <- sscopu(x,sym=TRUE,id=fit$id)
## Not run:
## Kendall's tau and Spearman's rho
summary(fit); summary(fit2); summary(fit.s)
## clean up
rm(x,fit,fit2,fit.s)
## End(Not run)</pre>
```

of Computational and Graphical Statistics, 24, 1053-1073.

sscox

Estimating Relative Risk Using Smoothing Splines

Description

Estimate relative risk using smoothing spline ANOVA models. The symbolic model specification via formula follows the same rules as in lm, but with the response of a special form.

Usage

```
sscox(formula, type=NULL, data=list(), weights=NULL, subset,
    na.action=na.omit, partial=NULL, alpha=1.4, id.basis=NULL,
    nbasis=NULL, seed=NULL, random=NULL, prec=1e-7, maxiter=30,
    skip.iter=FALSE)
```

Arguments

formula	Symbolic description of the model to be fit, where the response is of the form Surv(futime, status, start=0).
type	List specifying the type of spline for each variable. See mkterm for details.
data	Optional data frame containing the variables in the model.
weights	Optional vector of counts for duplicated data.
subset	Optional vector specifying a subset of observations to be used in the fitting pro-

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na.action	Function which indicates what should happen when the data contain NAs.
partial	Optional symbolic description of parametric terms in partial spline models.
alpha	Parameter defining cross-validation score for smoothing parameter selection.
id.basis	Index of observations to be used as "knots."
nbasis	Number of "knots" to be used. Ignored when id.basis is specified.
seed	Seed to be used for the random generation of "knots." Ignored when id.basis is specified.
random	Input for parametric random effects (frailty) in nonparametric mixed-effect models. See mkran for details.
prec	Precision requirement for internal iterations.
maxiter	Maximum number of iterations allowed for internal iterations.
skip.iter	Flag indicating whether to use initial values of theta and skip theta iteration. See ssanova for notes on skipping theta iteration.

Details

A proportional hazard model is assumed, and the relative risk is estimated via penalized partial likelihood. The model specification via formula is for the log relative risk. For example, Suve(t,d)~u*v prescribes a model of the form

$$log f(u, v) = g_u(u) + g_v(v) + g_{u,v}(u, v)$$

with the terms denoted by "u", "v", and "u:v"; relative risk is defined only up to a multiplicative constant, so the constant term is not included in the model.

sscox takes standard right-censored lifetime data, with possible left-truncation and covariates; in Surv(futime, status, start=0)~..., futime is the follow-up time, status is the censoring indicator, and start is the optional left-truncation time.

Parallel to those in a ssanova object, the model terms are sums of unpenalized and penalized terms. Attached to every penalized term there is a smoothing parameter, and the model complexity is largely determined by the number of smoothing parameters.

The selection of smoothing parameters is through a cross-validation mechanism designed for density estimation under biased sampling, with a fudge factor alpha; alpha=1 is "unbiased" for the minimization of Kullback-Leibler loss but may yield severe undersmoothing, whereas larger alpha yields smoother estimates.

A subset of the observations are selected as "knots." Unless specified via id.basis or nbasis, the number of "knots" q is determined by $max(30,10n^{2/9})$, which is appropriate for the default cubic splines for numerical vectors.

Value

sscox returns a list object of class "sscox".

The method predict.sscox can be used to evaluate the fits at arbitrary points along with standard errors. The method project.sscox can be used to calculate the Kullback-Leibler projection for model selection.

Note

The function Surv(futime, status, start=0) is defined and parsed inside sscox, not quite the same as the one in the survival package. The estimation is invariant of monotone transformations of time.

The results may vary from run to run. For consistency, specify id.basis or set seed.

References

```
Gu, C. (2013), Smoothing Spline ANOVA Models (2nd Ed). New York: Springer-Verlag. Gu, C. (2014), Smoothing Spline ANOVA Models: R Package gss. Journal of Statistical Software, 58(5), 1-25. URL http://www.jstatsoft.org/v58/i05/.
```

Examples

```
## Relative Risk
data(stan)
fit.rr <- sscox(Surv(futime,status)~age,data=stan)
est.rr <- predict(fit.rr,data.frame(age=c(35,40)),se=TRUE)
## Base Hazard
risk <- predict(fit.rr,stan)
fit.bh <- sshzd(Surv(futime,status)~futime,data=stan,offset=log(risk))
tt <- seq(0,max(stan$futime),length=51)
est.bh <- hzdcurve.sshzd(fit.bh,tt,se=TRUE)
## Clean up
## Not run: rm(stan,fit.rr,est.rr,risk,fit.bh,tt,est.bh)</pre>
```

ssden

Estimating Probability Density Using Smoothing Splines

Description

Estimate probability densities using smoothing spline ANOVA models. The symbolic model specification via formula follows the same rules as in 1m, but with the response missing.

Usage

```
ssden(formula, type=NULL, data=list(), alpha=1.4, weights=NULL,
    subset, na.action=na.omit, id.basis=NULL, nbasis=NULL, seed=NULL,
    domain=as.list(NULL), quad=NULL, qdsz.depth=NULL, bias=NULL,
    prec=1e-7, maxiter=30, skip.iter=FALSE)

ssden1(formula, type=NULL, data=list(), alpha=1.4, weights=NULL,
    subset, na.action=na.omit, id.basis=NULL, nbasis=NULL, seed=NULL,
    domain=as.list(NULL), quad=NULL, prec=1e-7, maxiter=30)
```

Symbolic description of the model to be fit.

Arguments

formula

domain

List specifying the type of spline for each variable. See mkterm for details. type Optional data frame containing the variables in the model. data alpha Parameter defining cross-validation score for smoothing parameter selection. Optional vector of bin-counts for histogram data. weights subset Optional vector specifying a subset of observations to be used in the fitting process. na.action Function which indicates what should happen when the data contain NAs. Index of observations to be used as "knots." id.basis nbasis Number of "knots" to be used. Ignored when id. basis is specified. Seed to be used for the random generation of "knots." Ignored when id.basis seed is specified.

Data frame specifying marginal support of density.

quad Quadrature for calculating integral. Mandatory if variables other than factors or

numerical vectors are involved.

qdsz.depth Depth to be used in smolyak.quad for the generation of quadrature.

bias Input for sampling bias.

prec Precision requirement for internal iterations.

maxiter Maximum number of iterations allowed for internal iterations.

skip.iter Flag indicating whether to use initial values of theta and skip theta iteration. See

ssanova for notes on skipping theta iteration.

Details

The model specification via formula is for the log density. For example, ~x1*x2 prescribes a model of the form

$$log f(x1, x2) = g_1(x1) + g_2(x2) + g_{12}(x1, x2) + C$$

with the terms denoted by "x1", "x2", and "x1:x2"; the constant is determined by the fact that a density integrates to one.

The selective term elimination may characterize (conditional) independence structures between variables. For example, $\sim x1*x2+x1*x3$ yields the conditional independence of x2 and x3 given x1

Parallel to those in a ssanova object, the model terms are sums of unpenalized and penalized terms. Attached to every penalized term there is a smoothing parameter, and the model complexity is largely determined by the number of smoothing parameters.

The selection of smoothing parameters is through a cross-validation mechanism described in the references, with a parameter alpha; alpha=1 is "unbiased" for the minimization of Kullback-Leibler loss but may yield severe undersmoothing, whereas larger alpha yields smoother estimates.

A subset of the observations are selected as "knots." Unless specified via id. basis or nbasis, the number of "knots" q is determined by $max(30, 10n^{2/9})$, which is appropriate for the default cubic splines for numerical vectors.

Value

ssden returns a list object of class "ssden". ssden1 returns a list object of class c("ssden1", "ssden").

dssden and cdssden can be used to evaluate the estimated joint density and conditional density; pssden, qssden, cpssden, and cqssden can be used to evaluate (conditional) cdf and quantiles.

The method project.ssden can be used to calculate the Kullback-Leibler projection of "ssden" objects for model selection; project.ssden1 can be used to calculate the square error projection of "ssden1" objects.

Note

In ssden, default quadrature will be constructed for numerical vectors on a hyper cube, then outer product with factor levels will be taken if factors are involved. The sides of the hyper cube are specified by domain; for domain\$x missing, the default is $c(\min(x), \max(x)) + c(-1, 1) * (\max(x) - \min(x)) * .05$. In 1-D, the quadrature is the 200-point Gauss-Legendre formula returned from gauss.quad. In multi-D, delayed Smolyak cubatures from smolyak.quad are used on cubes with the marginals properly transformed; see Gu and Wang (2003) for the marginal transformations.

For reasonable execution time in higher dimensions, set skip.iter=TRUE in call to ssden.

If you get an error message from ssden stating "Newton iteration diverges", try to use a larger qdsz.depth which will execute slower, or switch to ssden1. The default values of qdsz.depth for dimensions 4, 5, 6+ are 12, 11, 10.

ssden1 does not involve multi-D quadrature but does not perform as well as ssden. It can be used in very high dimensions where ssden is infeasible.

The results may vary from run to run. For consistency, specify id.basis or set seed.

Author(s)

Chong Gu, <chong@stat.purdue.edu>

References

Gu, C. and Wang, J. (2003), Penalized likelihood density estimation: Direct cross-validation and scalable approximation. *Statistica Sinica*, **13**, 811–826.

Gu, C., Jeon, Y., and Lin, Y. (2013), Nonparametric density estimation in high dimensions. *Statistica Sinica*, **23**, 1131–1153.

Gu, C. (2013), Smoothing Spline ANOVA Models (2nd Ed). New York: Springer-Verlag.

Gu, C. (2014), Smoothing Spline ANOVA Models: R Package gss. *Journal of Statistical Software*, 58(5), 1-25. URL http://www.jstatsoft.org/v58/i05/.

Examples

```
## 1-D estimate: Buffalo snowfall
data(buffalo)
buff.fit <- ssden(~buffalo,domain=data.frame(buffalo=c(0,150)))
plot(xx<-seq(0,150,len=101),dssden(buff.fit,xx),type="1")
plot(xx,pssden(buff.fit,xx),type="1")
plot(qq<-seq(0,1,len=51),qssden(buff.fit,qq),type="1")</pre>
```

```
## Clean up
## Not run: rm(buffalo,buff.fit,xx,qq)
dev.off()
## End(Not run)
## 2-D with triangular domain: AIDS incubation
data(aids)
## rectangular quadrature
quad.pt \leftarrow expand.grid(incu=((1:40)-.5)/40*100,infe=((1:40)-.5)/40*100)
quad.pt <- quad.pt[quad.pt$incu<=quad.pt$infe,]</pre>
quad.wt <- rep(1,nrow(quad.pt))</pre>
quad.wt[quad.pt$incu==quad.pt$infe] <- .5</pre>
quad.wt <- quad.wt/sum(quad.wt)*5e3
## additive model (pre-truncation independence)
aids.fit <- ssden(~incu+infe,data=aids,subset=age>=60,
                  domain=data.frame(incu=c(0,100),infe=c(0,100)),
                  quad=list(pt=quad.pt,wt=quad.wt))
## conditional (marginal) density of infe
jk <- cdssden(aids.fit,xx<-seq(0,100,len=51),data.frame(incu=50))</pre>
plot(xx,jk$pdf,type="1")
## conditional (marginal) quantiles of infe (TIME-CONSUMING)
## Not run:
cqssden(aids.fit,c(.05,.25,.5,.75,.95),data.frame(incu=50))
## End(Not run)
## Clean up
## Not run: rm(aids,quad.pt,quad.wt,aids.fit,jk,xx)
dev.off()
## End(Not run)
## One factor plus one vector
data(gastric)
gastric$trt
fit <- ssden(~futime*trt,data=gastric)</pre>
## conditional density
cdssden(fit,c("1","2"),cond=data.frame(futime=150))
## conditional quantiles
cqssden(fit,c(.05,.25,.5,.75,.95),data.frame(trt=as.factor("1")))\\
## Clean up
## Not run: rm(gastric,fit)
## Sampling bias
## (X,T) is truncated to T<X<1 for T~U(0,1), so X is length-biased
rbias <- function(n) {</pre>
 t <- runif(n)
 x <- rnorm(n, .5, .15)
 ok <- (x>t)&(x<1)
 while(m<-sum(!ok)) {</pre>
    t[!ok] <- runif(m)
   x[!ok] <- rnorm(m, .5, .15)
    ok <- (x>t)&(x<1)
 cbind(x,t)
```

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```
}
xt <- rbias(100)
x <- xt[,1]; t <- xt[,2]
## length-biased
bias1 <- list(t=1,wt=1,fun=function(t,x){x[,]})
fit1 <- ssden(~x,domain=list(x=c(0,1)),bias=bias1)
plot(xx<-seq(0,1,len=101),dssden(fit1,xx),type="1")
## truncated
bias2 <- list(t=t,wt=rep(1/100,100),fun=function(t,x){x[,]>t})
fit2 <- ssden(~x,domain=list(x=c(0,1)),bias=bias2)
plot(xx,dssden(fit2,xx),type="1")
## Clean up
## Not run: rm(rbias,xt,x,t,bias1,fit1,bias2,fit2)</pre>
```

sshzd

Estimating Hazard Function Using Smoothing Splines

Description

Estimate hazard function using smoothing spline ANOVA models. The symbolic model specification via formula follows the same rules as in lm, but with the response of a special form.

Usage

```
sshzd(formula, type=NULL, data=list(), alpha=1.4, weights=NULL,
    subset, offset, na.action=na.omit, partial=NULL, id.basis=NULL,
    nbasis=NULL, seed=NULL, random=NULL, prec=1e-7, maxiter=30,
    skip.iter=FALSE)

sshzd1(formula, type=NULL, data=list(), alpha=1.4, weights=NULL,
    subset, na.action=na.omit, rho="marginal", partial=NULL,
    id.basis=NULL, nbasis=NULL, seed=NULL, random=NULL, prec=1e-7,
    maxiter=30, skip.iter=FALSE)
```

Arguments

formula	Symbolic description of the model to be fit, where the response is of the form Surv(futime, status, start=0).
type	List specifying the type of spline for each variable. See mkterm for details.
data	Optional data frame containing the variables in the model.
alpha	Parameter defining cross-validation score for smoothing parameter selection.
weights	Optional vector of counts for duplicated data.
subset	Optional vector specifying a subset of observations to be used in the fitting process.
offset	Optional offset term with known parameter 1.
na.action	Function which indicates what should happen when the data contain NAs.

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partial Optional symbolic description of parametric terms in partial spline models.

id.basis Index of observations to be used as "knots."

nbasis Number of "knots" to be used. Ignored when id.basis is specified.

seed Seed to be used for the random generation of "knots." Ignored when id.basis

is specified.

random Input for parametric random effects (frailty) in nonparametric mixed-effect mod-

els. See mkran for details.

prec Precision requirement for internal iterations.

maxiter Maximum number of iterations allowed for internal iterations.

skip.iter Flag indicating whether to use initial values of theta and skip theta iteration. See

ssanova for notes on skipping theta iteration.

rho Choice of rho function for sshzd1: "marginal" or "weibull".

Details

The model specification via formula is for the log hazard. For example, $Suve(t,d)^*t*u$ prescribes a model of the form

$$log f(t, u) = C + g_t(t) + g_u(u) + g_{t,u}(t, u)$$

with the terms denoted by "1", "t", "u", and "t:u". Replacing t*u by t+u in the formula, one gets a proportional hazard model with $g_{t,u}=0$.

sshzd takes standard right-censored lifetime data, with possible left-truncation and covariates; in Surv(futime, status, start=0)~..., futime is the follow-up time, status is the censoring indicator, and start is the optional left-truncation time. The main effect of futime must appear in the model terms specified via

Parallel to those in a ssanova object, the model terms are sums of unpenalized and penalized terms. Attached to every penalized term there is a smoothing parameter, and the model complexity is largely determined by the number of smoothing parameters.

The selection of smoothing parameters is through a cross-validation mechanism described in Gu (2002, Sec. 7.2), with a parameter alpha; alpha=1 is "unbiased" for the minimization of Kullback-Leibler loss but may yield severe undersmoothing, whereas larger alpha yields smoother estimates.

A subset of the observations are selected as "knots." Unless specified via id.basis or nbasis, the number of "knots" q is determined by $max(30,10n^{2/9})$, which is appropriate for the default cubic splines for numerical vectors.

Value

sshzd returns a list object of class "sshzd". sshzd1 returns a list object of class c("sshzd1", "sshzd").

hzdrate.sshzd can be used to evaluate the estimated hazard function. hzdcurve.sshzd can be used to evaluate hazard curves with fixed covariates. survexp.sshzd can be used to calculated estimated expected survival.

The method project.sshzd can be used to calculate the Kullback-Leibler projection of "sshzd" objects for model selection; project.sshzd1 can be used to calculate the square error projection of "sshzd1" objects.

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Note

The function Surv(futime, status, start=0) is defined and parsed inside sshzd, not quite the same as the one in the survival package.

Integration on the time axis is done by the 200-point Gauss-Legendre formula on c(min(start), max(futime)), returned from gauss.quad.

sshzd1 can be up to 50 times faster than sshzd, at the cost of performance degradation.

The results may vary from run to run. For consistency, specify id.basis or set seed.

References

Du, P. and Gu, C. (2006), Penalized likelihood hazard estimation: efficient approximation and Bayesian confidence intervals. *Statistics and Probability Letters*, **76**, 244–254.

Du, P. and Gu, C. (2009), Penalized Pseudo-Likelihood Hazard Estimation: A Fast Alternative to Penalized Likelihood. *Journal of Statistical Planning and Inference*, **139**, 891–899.

Du, P. and Ma, S. (2010), Frailty Model with Spline Estimated Nonparametric Hazard Function, *Statistica Sinica*, **20**, 561–580.

Gu, C. (2013), Smoothing Spline ANOVA Models (2nd Ed). New York: Springer-Verlag.

Gu, C. (2014), Smoothing Spline ANOVA Models: R Package gss. *Journal of Statistical Software*, 58(5), 1-25. URL http://www.jstatsoft.org/v58/i05/.

Examples

```
## Model with interaction
data(gastric)
gastric.fit <- sshzd(Surv(futime, status)~futime*trt, data=gastric)</pre>
\# exp(-Lambda(600)), exp(-(Lambda(1200)-Lambda(600))), and exp(-Lambda(1200))
survexp.sshzd(gastric.fit,c(600,1200,1200),data.frame(trt=as.factor(1)),c(0,600,0))
## Clean up
## Not run: rm(gastric,gastric.fit)
dev.off()
## End(Not run)
## THE FOLLOWING EXAMPLE IS TIME-CONSUMING
## Proportional hazard model
## Not run:
data(stan)
stan.fit <- sshzd(Surv(futime, status)~futime+age, data=stan)</pre>
## Evaluate fitted hazard
hzdrate.sshzd(stan.fit,data.frame(futime=c(10,20),age=c(20,30)))
## Plot lambda(t,age=20)
tt <- seq(0,60,leng=101)
hh <- hzdcurve.sshzd(stan.fit,tt,data.frame(age=20))</pre>
plot(tt,hh,type="l")
## Clean up
rm(stan, stan.fit, tt, hh)
dev.off()
## End(Not run)
```

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sshzd2d	Estimating 2-D Hazard Function Using Smoothing Splines

Description

Estimate 2-D hazard function using smoothing spline ANOVA models.

Usage

```
sshzd2d(formula1, formula2, symmetry=FALSE, data, alpha=1.4,
    weights=NULL, subset=NULL, id.basis=NULL, nbasis=NULL, seed=NULL,
    prec=1e-7, maxiter=30, skip.iter=FALSE)

sshzd2d1(formula1, formula2, symmetry=FALSE, data, alpha=1.4,
    weights=NULL, subset=NULL, rho="marginal",
    id.basis=NULL, nbasis=NULL, seed=NULL, prec=1e-7, maxiter=30,
    skip.iter=FALSE)
```

Arguments

formula1	Description of the hazard model to be fit on the first axis.	
formula2	Description of the hazard model to be fit on the second axis.	
symmetry	Flag indicating whether to enforce symmetry of the two axes.	
data	Data frame containing the variables in the model.	
alpha	Parameter defining cross-validation scores for smoothing parameter selection.	
weights	Optional vector of counts for duplicated data.	
subset	Optional vector specifying a subset of observations to be used in the fitting process.	
id.basis	Index of observations to be used as "knots."	
nbasis	Number of "knots" to be used. Ignored when id.basis is specified.	
seed	Seed to be used for the random generation of "knots." Ignored when id.basis is specified.	
prec	Precision requirement for internal iterations.	
maxiter	Maximum number of iterations allowed for internal iterations.	
skip.iter	Flag indicating whether to use initial values of theta and skip theta iteration in marginal hazard estimation.	
rho	Choice of rho function for sshzd2d1: "marginal" or "weibull".	

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Details

The 2-D survival function is expressed as S(t1,t2) = C(S1(t1),S2(t2)), where S1(t1),S2(t2) are marginal survival functions and C(u1,u2) is a 2-D copula. The marginal survival functions are estimated via the marginal hazards as in sshzd, and the copula is estimated nonparametrically by calling sscopu2.

When symmetry=TRUE, a common marginal survial function S1(t)=S2(t) is estimated, and a symmetric copula is estimated such that C(u1, u2) = C(u2, u1).

Covariates can be incorporated in the marginal hazard models as in sshzd, including parametric terms via partial and frailty terms via random. Arguments formula1 and formula2 are typically model formulas of the same form as the argument formula in sshzd, but when partial or random are needed, formula1 and formula2 should be lists with model formulas as the first elements and partial/random as named elements; when necessary, variable configurations (that are done via argument type in sshzd) should also be entered as named elements of lists formula1/formula2.

When symmetry=TRUE, parallel model formulas must be consistent of each other, such as

```
formula1=list(Surv(t1,d1)~t1*u1,partial=~z1,random=~1|id1)
formula2=list(Surv(t2,d2)~t2*u2,partial=~z2,random=~1|id2)
```

where pairs t1-t2, d2-d2 respectively are different elements in data, pairs u1-u2, z1-z2 respectively may or may not be different elements in data, and factors id1 and id2 are typically the same but at least should have the same levels.

Value

sshzd2d and sshzd2d1 return a list object of class "sshzd2d".

hzdrate.sshzd2d can be used to evaluate the estimated 2-D hazard function. survexp.sshzd2d can be used to calculate estimated survival functions.

Note

sshzd2d1 executes faster than sshzd2d, but often at the cost of performance degradation.

The results may vary from run to run. For consistency, specify id.basis or set seed.

Author(s)

Chong Gu, <chong@stat.purdue.edu>

References

Gu, C. (2015), Hazard estimation with bivariate survival data and copula density estimation. *Journal of Computational and Graphical Statistics*, **24**, 1053-1073.

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Examples

```
## THE FOLLOWING EXAMPLE IS TIME-CONSUMING
## Not run:
data(DiaRet)
## Common proportional hazard model on the margins
fit <- sshzd2d(Surv(time1, status1)~time1+trt1*type,</pre>
               Surv(time2, status2)~time2+trt2*type,
               data=DiaRet,symmetry=TRUE)
## Evaluate fitted survival and hazard functions
time <- cbind(c(50,70),c(70,70))
cova <- data.frame(trt1=as.factor(c(1,1)),trt2=as.factor(c(1,0)),
                   type=as.factor(c("juvenile","adult")))
survexp.sshzd2d(fit,time,cov=cova)
hzdrate.sshzd2d(fit,time,cov=cova)
## Association between margins: Kendall's tau and Spearman's rho
summary(fit$copu)
## Clean up
rm(DiaRet,fit,time,cova)
dev.off()
## End(Not run)
```

ssllrm

Fitting Smoothing Spline Log-Linear Regression Models

Description

Fit smoothing spline log-linear regression models. The symbolic model specification via formula follows the same rules as in 1m.

Usage

Arguments

formula	Symbolic description of the model to be fit.
response	Formula listing response variables.
type	List specifying the type of spline for each variable. See mkterm for details.
data	Optional data frame containing the variables in the model.
weights	Optional vector of weights to be used in the fitting process.
subset	Optional vector specifying a subset of observations to be used in the fitting process.
na.action	Function which indicates what should happen when the data contain NAs.

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alpha	Parameter modifying GCV or Mallows' CL; larger absolute values yield smoother fits; negative value invokes a stable and more accurate GCV/CL evaluation algorithm but may take two to five times as long. Ignored when method="m" are specified.	
id.basis	Index designating selected "knots".	
nbasis	Number of "knots" to be selected. Ignored when id. basis is supplied.	
seed	Seed to be used for the random generation of "knots". Ignored when id.basis is supplied.	
random	Input for parametric random effects in nonparametric mixed-effect models. See mkran for details.	
prec	Precision requirement for internal iterations.	
maxiter	Maximum number of iterations allowed for internal iterations.	
skip.iter	Flag indicating whether to use initial values of theta and skip theta iteration. See ssanova for notes on skipping theta iteration.	

Details

The model is specified via formula and response, where response lists the response variables. For example, ssllrm(~y1*y2*x,~y1+y2) prescribe a model of the form

$$log f(y1, y2|x) = g_1(y1) + g_2(y2) + g_{12}(y1, y2) + g_{x1}(x, y1) + g_{x2}(x, y2) + g_{x12}(x, y1, y2) + C(x)$$

with the terms denoted by "y1", "y2", "y1:y2", "y1:x", "y2:x", and "y1:y2:x"; the term(s) not involving response(s) are removed and the constant C(x) is determined by the fact that a conditional density integrates (adds) to one on the y axis.

The model terms are sums of unpenalized and penalized terms. Attached to every penalized term there is a smoothing parameter, and the model complexity is largely determined by the number of smoothing parameters.

A subset of the observations are selected as "knots." Unless specified via id.basis or nbasis, the number of "knots" q is determined by $max(30,10n^{2/9})$, which is appropriate for the default cubic splines for numerical vectors.

Value

ssllrm returns a list object of class "ssllrm".

The method predict.ssllrm can be used to evaluate f(y|x) at arbitrary x, or contrasts of $log\{f(y|x)\}$ such as the odds ratio along with standard errors. The method project.ssllrm can be used to calculate the Kullback-Leibler projection for model selection.

Note

The responses, or y-variables, must be factors, and there must be at least one numerical x's. For response, there is no difference between \sim y1+y2 and \sim y1*y2.

The results may vary from run to run. For consistency, specify id.basis or set seed.

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References

Gu, C. and Ma, P. (2011), Nonparametric regression with cross-classified responses. *The Canadian Journal of Statistics*, **39**, 591–609.

Gu, C. (2014), Smoothing Spline ANOVA Models: R Package gss. *Journal of Statistical Software*, 58(5), 1-25. URL http://www.jstatsoft.org/v58/i05/.

Examples

```
## Simulate data
test <- function(x)</pre>
        \{.3*(1e6*(x^11*(1-x)^6)+1e4*(x^3*(1-x)^10))-2\}
x < -(0:100)/100
p <- 1-1/(1+exp(test(x)))
y \leftarrow rbinom(x,3,p)
y1 <- as.ordered(y)</pre>
y2 <- as.factor(rbinom(x,1,p))
## Fit model
fit <- ssllrm(\simy1\timesy2\timesx,\simy1+y2)
## Evaluate f(y|x)
est <- predict(fit,data.frame(x=x),</pre>
                data.frame(y1=as.factor(0:3), y2=as.factor(rep(0,4))))
## f(y|x) at all y values (fit$qd.pt)
est <- predict(fit,data.frame(x=x))</pre>
## Evaluate contrast of log f(y|x)
est <- predict(fit,data.frame(x=x),odds=c(-1,.5,.5,0),</pre>
                data.frame(y1=as.factor(0:3), y2=as.factor(rep(0,4))), se=TRUE)
## Odds ratio log\{f(0,0|x)/f(3,0|x)\}
est <- predict(fit,data.frame(x=x),odds=c(1,-1),</pre>
                data.frame(y1=as.factor(c(0,3)),y2=as.factor(c(0,1))),se=TRUE)
## KL projection
kl <- project(fit,include=c("y2:x","y1:y2","y1:x","y2:x"))</pre>
## Clean up
## Not run: rm(test,x,p,y,y1,y2,fit,est,kl)
dev.off()
## End(Not run)
```

stan

Stanford Heart Transplant Data

Description

Survival of patients from the Stanford heart transplant program.

Usage

```
data(stan)
```

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Format

A data frame containing 184 observations on the following variables.

time Follow-up time after transplant, in days.

status Censoring status.
age Age at transplant.
futime Square root of time.

Source

Miller, R. G. and Halpern, J. (1982), Regression with censored data. *Biometrika*, 69, 521–531.

summary.gssanova Assessing Smoothing Spline ANOVA Fits with Non-Gaussian Responses

Description

Calculate various summaries of smoothing spline ANOVA fits with non-Gaussian responses.

Usage

```
## S3 method for class 'gssanova'
summary(object, diagnostics=FALSE, ...)
```

Arguments

object Object of class "gssanova".

diagnostics Flag indicating if diagnostics are required.

... Ignored.

Details

Similar to the iterated weighted least squares fitting of glm, penalized likelihood regression fit can be calculated through iterated penalized weighted least squares.

The diagnostics are based on the "pseudo" Gaussian response model behind the weighted least squares problem at convergence.

Value

 $summary. gss an ova\ returns\ a\ list\ object\ of\ class\ "summary. gss an ova"\ consisting\ of\ the\ following\ elements.$ The entries pi, kappa, cosines, and roughness are only calculated if diagnostics=TRUE.

call Fitting call.

family Error distribution.

alpha Parameter used to define cross-validation in model fitting.

64 summary.gssanova0

fitted Fitted values on the link scale.

dispersion Assumed or estimated dispersion parameter.

residuals Working residuals on the link scale.

rss Residual sum of squares.

dev.resid Deviance residuals.
deviance Deviance of the fit.

dev.null Deviance of the null model.

penalty Roughness penalty associated with the fit.

pi "Percentage decomposition" of "explained variance" into model terms.

kappa Concurvity diagnostics for model terms. Virtually the square roots of variance

inflation factors of a retrospective linear model.

cosines Cosine diagnostics for practical significance of model terms.

roughness Percentage decomposition of the roughness penalty penalty into model terms.

References

Gu, C. (1992), Diagnostics for nonparametric regression models with additive terms. *Journal of the American Statistical Association*, **87**, 1051–1058.

See Also

Fitting function gssanova and methods predict.ssanova, project.gssanova, fitted.gssanova.

summary.gssanova0 Assessing Smoothing Spline ANOVA Fits with Non-Gaussian Responses

Description

Calculate various summaries of smoothing spline ANOVA fits with non-Gaussian responses.

Usage

```
## S3 method for class 'gssanova0'
summary(object, diagnostics=FALSE, ...)
```

Arguments

object Object of class "gssanova".

diagnostics Flag indicating if diagnostics are required.

... Ignored.

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Details

Similar to the iterated weighted least squares fitting of glm, penalized likelihood regression fit can be calculated through iterated penalized weighted least squares.

The diagnostics are based on the "pseudo" Gaussian response model behind the weighted least squares problem at convergence.

Value

summary.gssanova0 returns a list object of class "summary.gssanova0" consisting of the following elements. The entries pi, kappa, cosines, and roughness are only calculated if diagnostics=TRUE.

call Fitting call.

family Error distribution.

method Method for smoothing parameter selection.

dispersion Assumed or estimated dispersion parameter.

iter Number of performance-oriented iterations performed.

fitted Fitted values on the link scale.

residuals Working residuals on the link scale.

rss Residual sum of squares.

dev.resid Deviance residuals.

deviance Deviance of the fit.

dev.null Deviance of the null model.

alpha Estimated size for family="nbinomial" with one column responses. Esti-

mated inverse scale of log life time for family="nbinomial", "lognorm", or

"loglogis".

penalty Roughness penalty associated with the fit.

pi "Percentage decomposition" of "explained variance" into model terms.

kappa Concurvity diagnostics for model terms. Virtually the square roots of variance

inflation factors of a retrospective linear model.

cosines Cosine diagnostics for practical significance of model terms.

roughness Percentage decomposition of the roughness penalty penalty into model terms.

References

Gu, C. (1992), Diagnostics for nonparametric regression models with additive terms. *Journal of the American Statistical Association*, **87**, 1051–1058.

See Also

Fitting function gssanova0 and methods predict.ssanova0, fitted.gssanova.

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summary.ssanova

Assessing Smoothing Spline ANOVA Fits

Description

Calculate various summaries of smoothing spline ANOVA fits.

Usage

```
## S3 method for class 'ssanova'
summary(object, diagnostics=FALSE, ...)
## S3 method for class 'ssanova0'
summary(object, diagnostics=FALSE, ...)
## S3 method for class 'ssanova9'
summary(object, diagnostics=FALSE, ...)
```

Arguments

object Object of class "ssanova".

diagnostics Flag indicating if diagnostics are required.

... Ignored.

Value

summary.ssanova returns a list object of class "summary.ssanova" consisting of the following elements. The entries pi, kappa, cosines, and roughness are only calculated if diagnostics=TRUE; see the reference below for details concerning the diagnostics.

call Fitting call.

method Method for smoothing parameter selection.

fitted Fitted values.
residuals Residuals.

sigma Assumed or estimated error standard deviation.

r.squared Fraction of "explained variance" by the fitted model.

rss Residual sum of squares.

penalty Roughness penalty associated with the fit.

pi "Percentage decomposition" of "explained variance" into model terms.

kappa Concurvity diagnostics for model terms. Virtually the square roots of variance

inflation factors of a retrospective linear model.

cosines Cosine diagnostics for practical significance of model terms.

roughness Percentage decomposition of the roughness penalty penalty into model terms.

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References

Gu, C. (1992), Diagnostics for nonparametric regression models with additive terms. *Journal of the American Statistical Association*, **87**, 1051–1058.

See Also

Fitting functions ssanova, ssanova@ and methods predict.ssanova, project.ssanova, fitted.ssanova.

summary.sscopu

Calculating Kendall's Tau and Spearman's Rho for 2-D Copula Density Estimates

Description

Calculate Kendall's tau and Spearman's rho for 2-D copula density estimates.

Usage

```
## S3 method for class 'sscopu'
summary(object, ...)
```

Arguments

```
object Object of class "sscopu".
... Ignored.
```

Value

A list containing Kendall's tau and Spearman's rho.

See Also

Fitting functions sscopu and sscopu2.

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wesdr

Progression of Diabetic Retinopathy

Description

Data derived from the Wisconsin Epidemiological Study of Diabetic Retinopathy.

Usage

data(wesdr)

Format

A data frame containing 669 observations on the following variables.

dur Duration of diabetes at baseline, in years.

gly Percent of glycosylated hemoglobin at baseline.

bmi Body mass index at baseline.

ret Binary indicator of retinopathy progression at first follow-up.

Source

Wang, Y. (1997), GRKPACK: Fitting smoothing spline ANOVA models for exponential families. *Communications in Statistics – Simulations and Computation*, **26**, 765–782.

References

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wesdr1 69

wesdr1

Stages of Diabetic Retinopathy

Description

Data derived from the Wisconsin Epidemiological Study of Diabetic Retinopathy.

Usage

data(wesdr1)

Format

A data frame containing 2049 observations on the following variables.

age	Age of patient.
dur	Duration of diabetes, in years.
gly	Percent of glycosylated hemoglobin
upro	Ordinal urine protein level.
insl	Binary indicator of insulin usage.
ret1	Ordinal retinopathy stage, right eye.
ret2	Ordinal retinopathy stage, left eye.

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